



Super-resolution of satellite observations of sea ice thickness using diffusion models and physical modeling

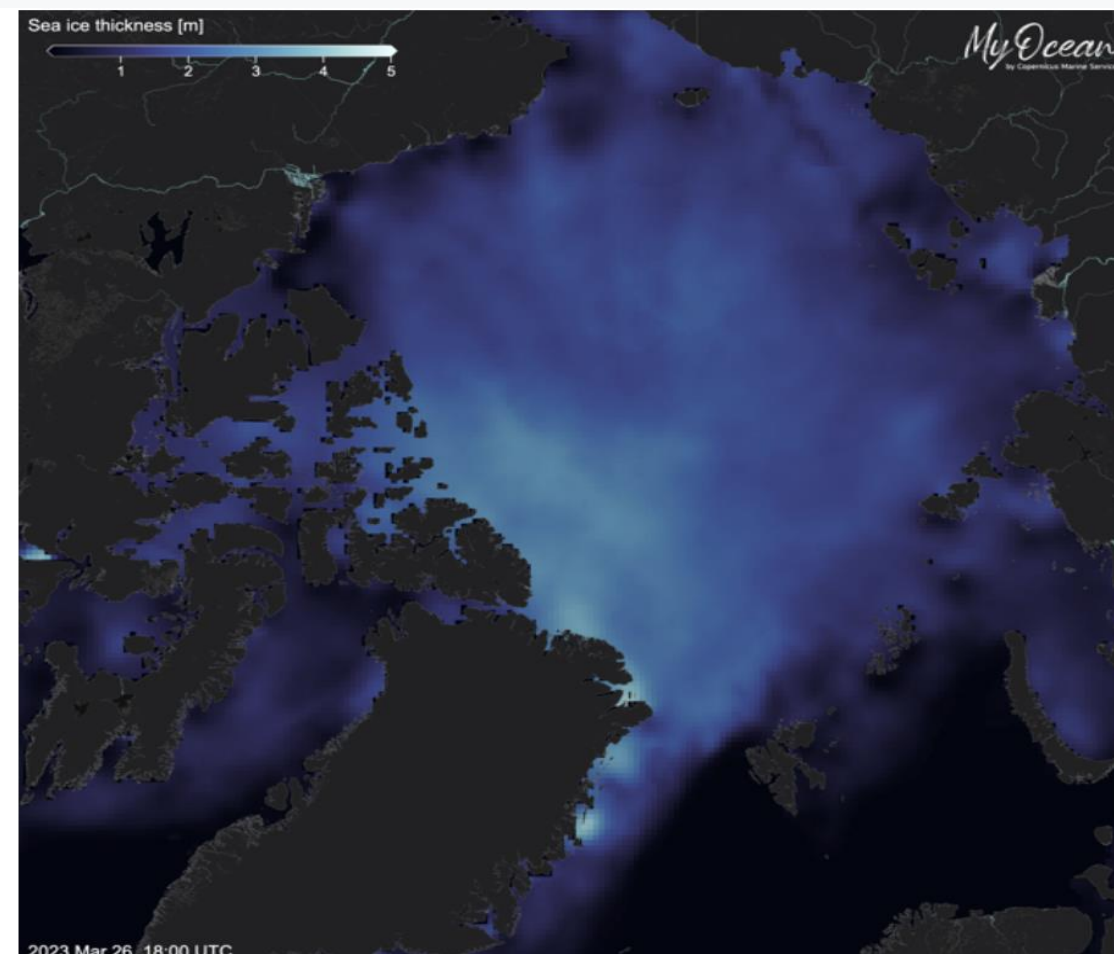
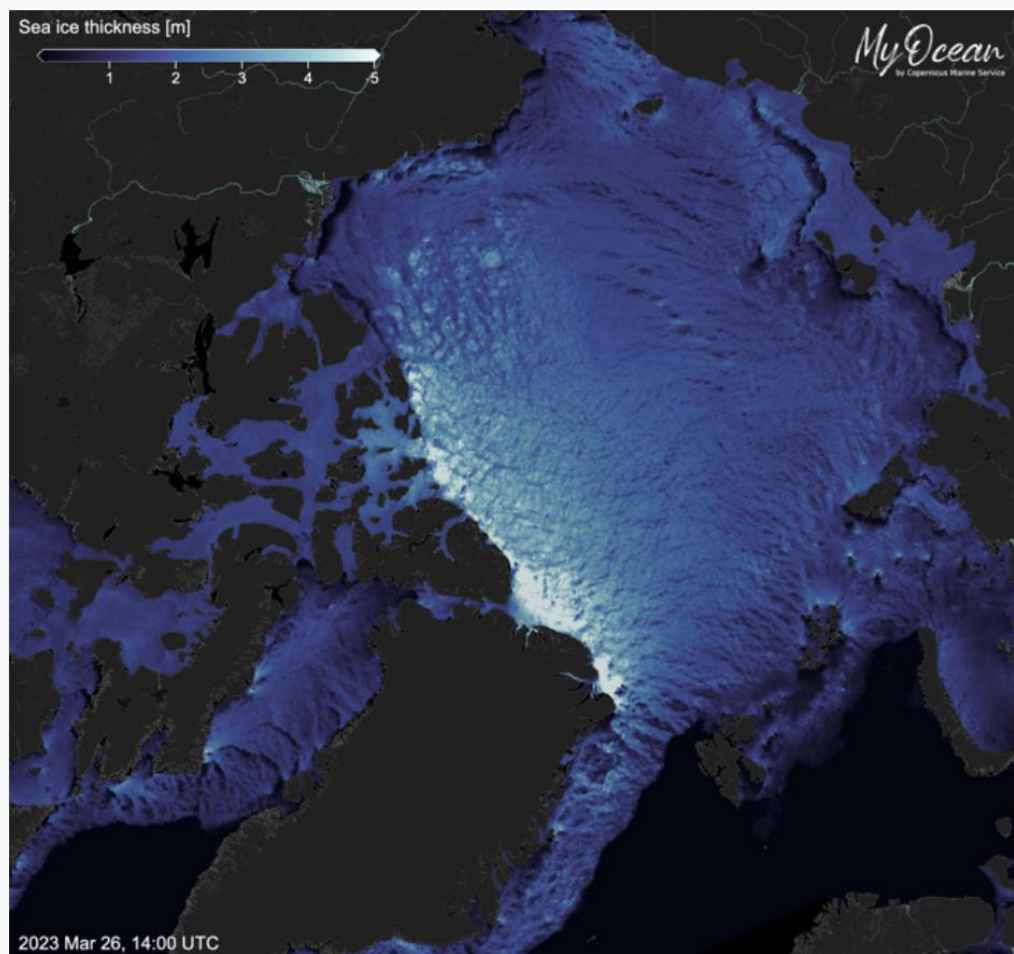
Julien Brajard, Anton Korosov, Fabio Mangini, Adrien Perrin, Richard Davy, and Yiguo Wang



Context

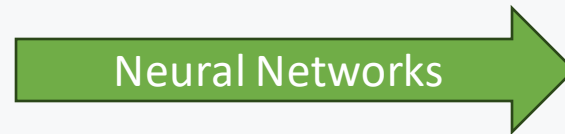
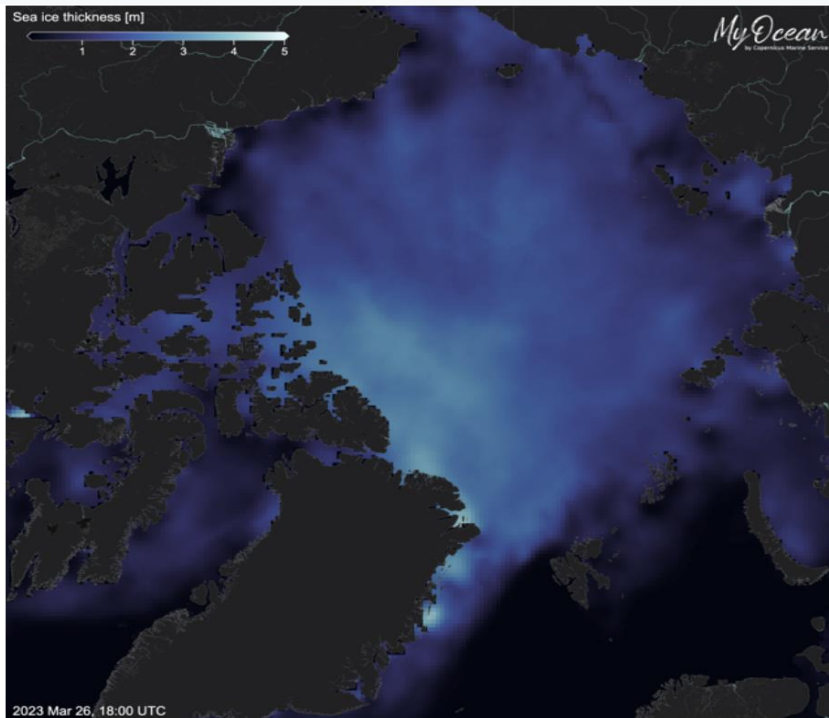
High-resolution model simulation of Sea ice thickness
in the Arctic
(3 km resolution)

The resolution we can observe
(~90 km resolution)

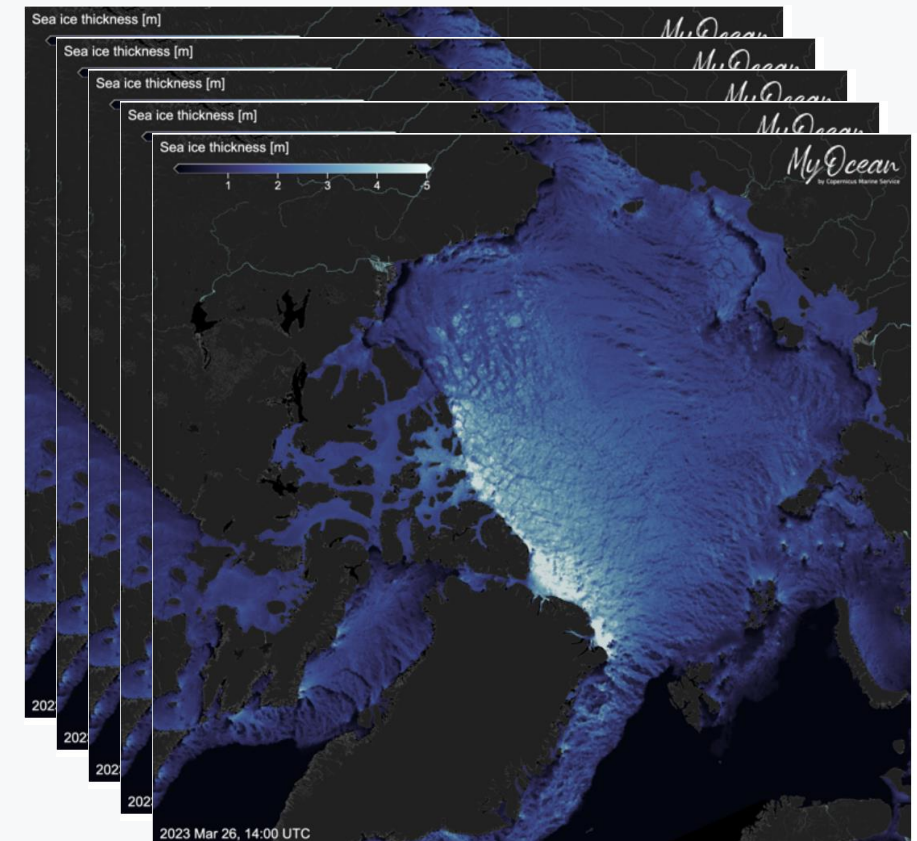


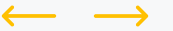
Objective of SuperIce

Low resolution image of sea ice thickness



High-resolution images





We use **diffusion models** to generate an ensemble of high-resolution sea ice thickness.

Good **accuracy** and **realism** of the generated fields.

Please visit my poster for more details **#13**

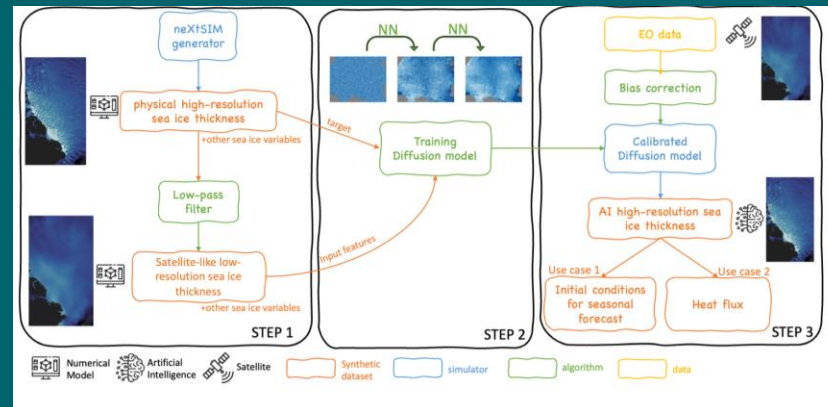
Super-resolution



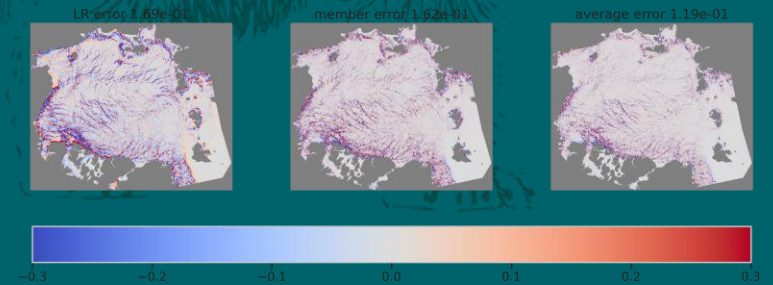
Motivation



Sketch of the project

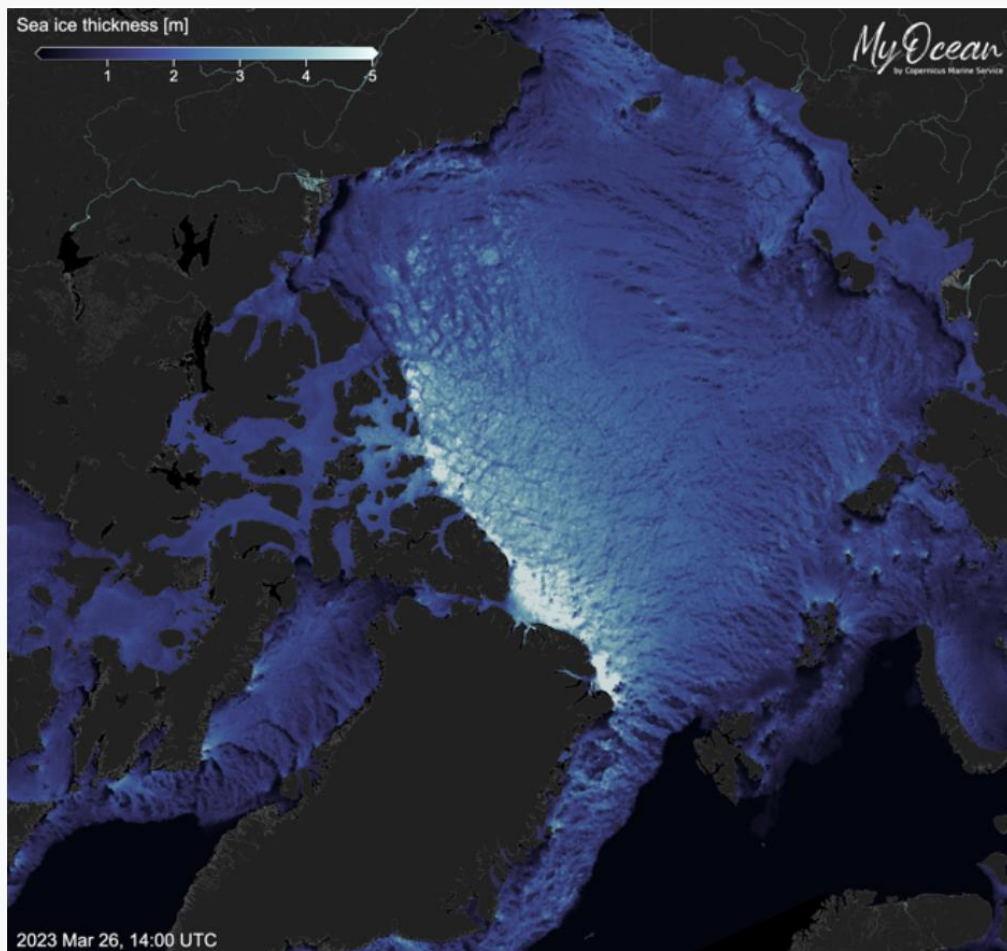


Results

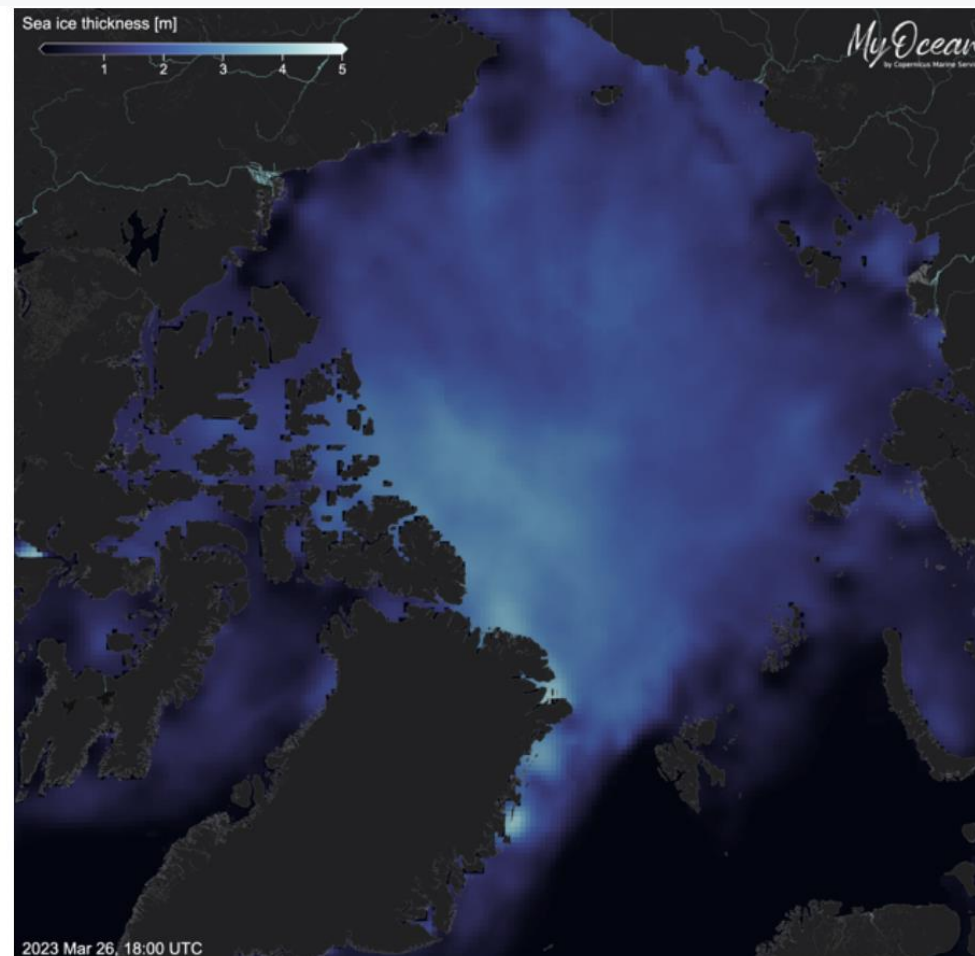


Motivation

Physical model (NeXtSIM) forecast



Satellite observation product (CS2SMOS)



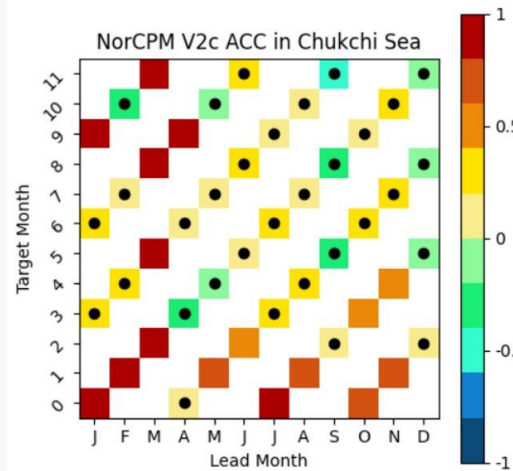
Satellite product does not resolve small scales in sea ice thickness (e.g. leads)

Why is it important?

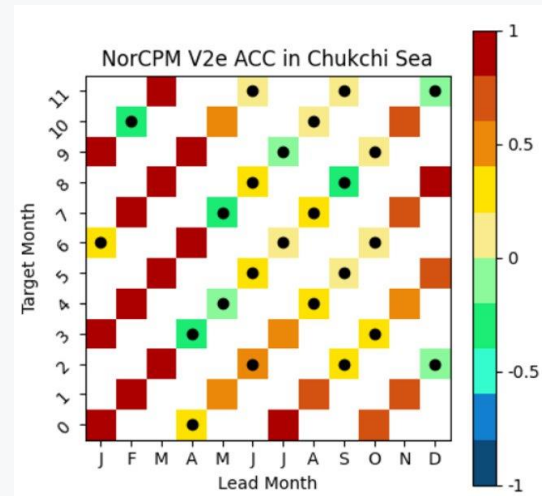
Case 1: Predictability

Forecast skill

Detrended correlation coefficient of Sea ice extent in Chukchi Sea



Initialization using Sea ice concentration observations only

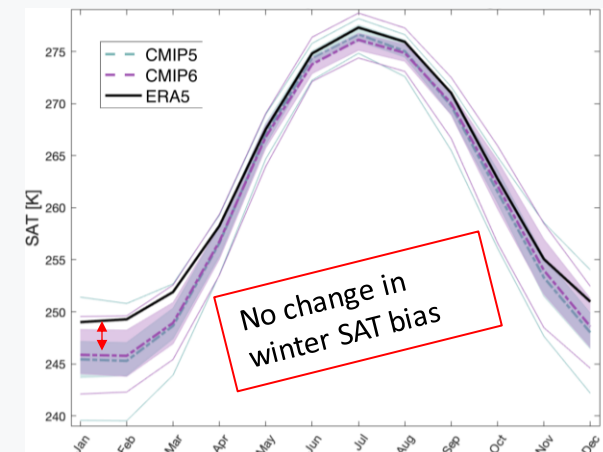
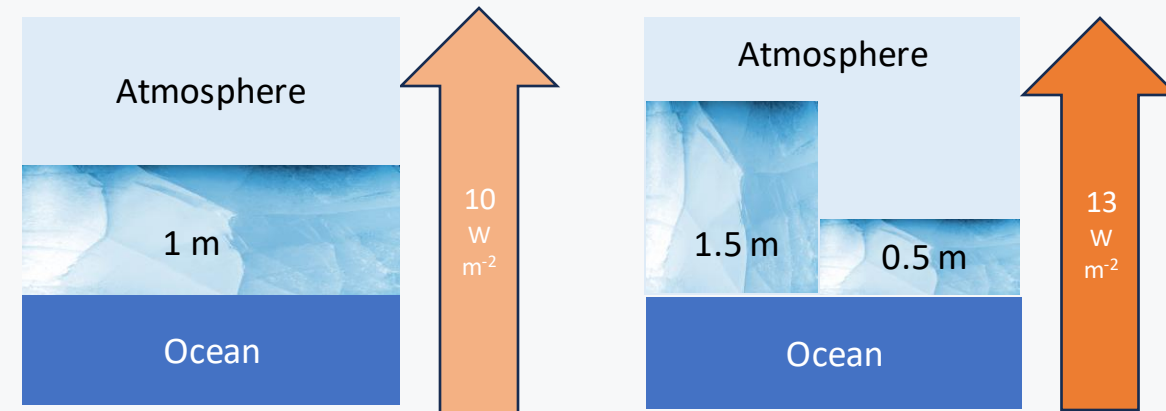


Initialization using Sea ice concentration observations + Sea ice thickness only

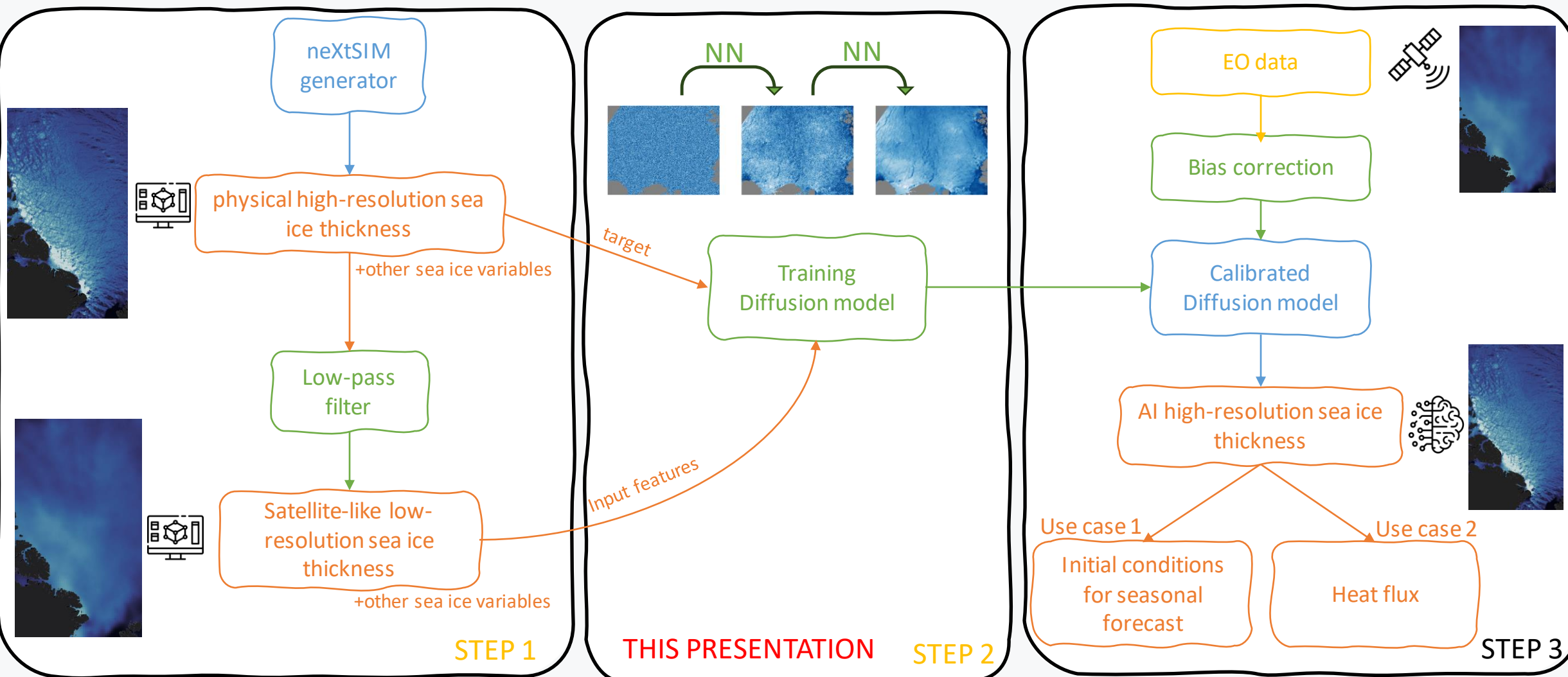
Black dot means not significant

Courtesy of N. Williams

Case 2: Surface fluxes



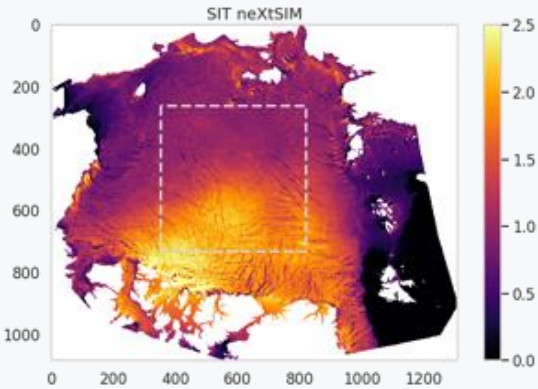
Overview of the project



Step 1: Dataset constitution

Principle: Filtering of NeXtSIM simulations

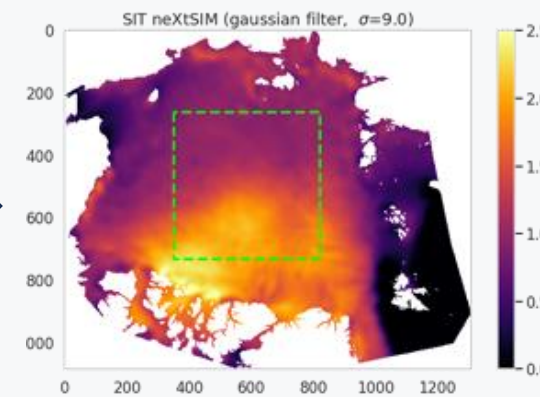
NeXtSIM sea ice thickness
01-01-2021 (res 3km)



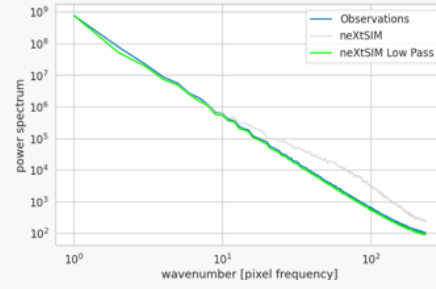
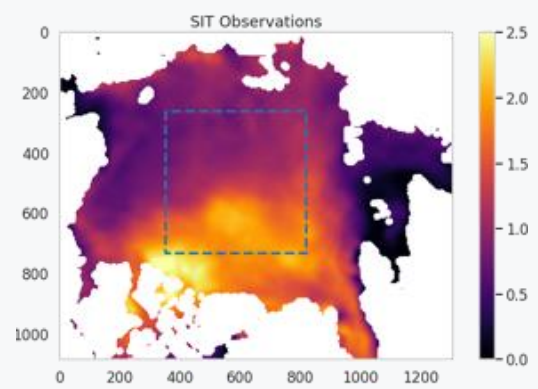
Convolution constant kernel (size 120 km)



Filtered sea ice thickness
(res ~ 90 km)

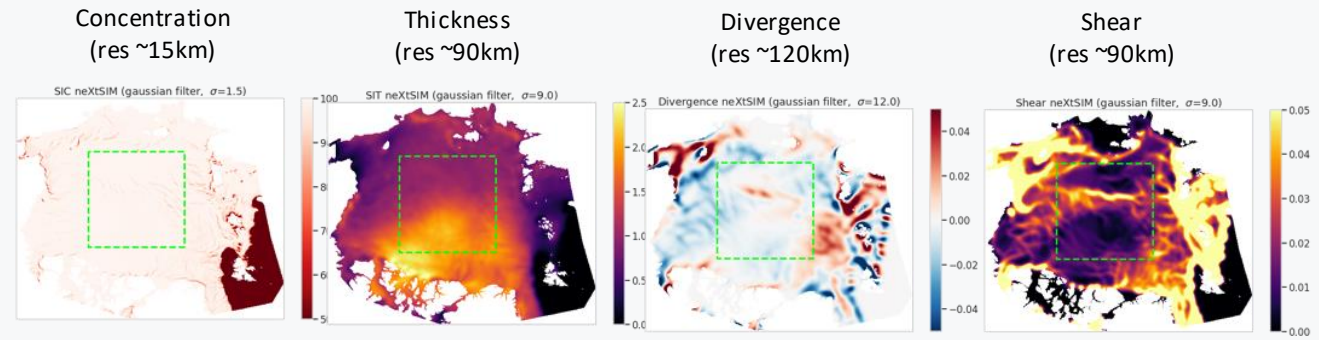


Observation product (CS2SMOS)
01-01-2021



Dataset:

- 5 input features (low-pass filtered) 1086x1308
- 529 samples, from 18-10-2013 to 15-04-2023 (Only Oct-Apr)
- Training: 2013-> Apr. 2020 (1157 samples)
- Validation/test Oct. Oct. 2020-> 2023 (540 samples)



+ land mask
(res ~3km, no smoothing)

Apply diffusion model to sea ice thickness super-resolution

Used for AI image generator (Ex: Midjourney)

A prompt

“man walking dog at dusk --ar 4:3”

Generative
diffusion model



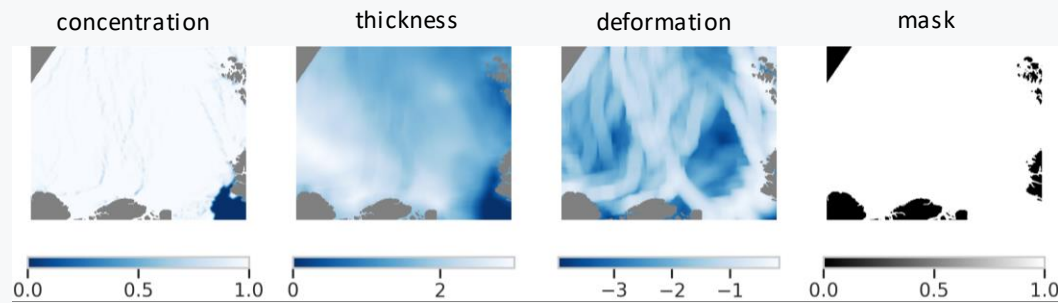
A generated image



Apply diffusion model to sea ice thickness super-resolution

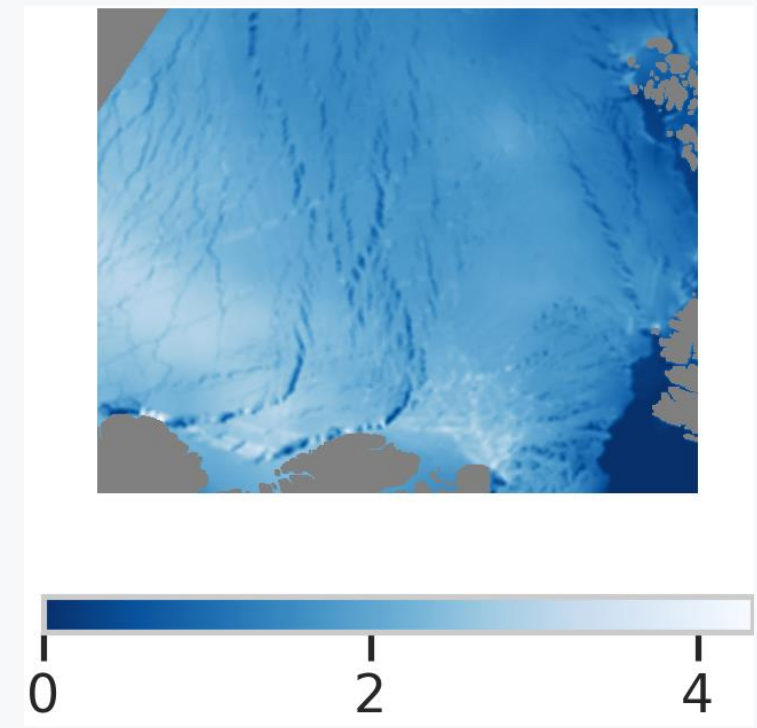
Used for AI image generator (Ex: Midjourney)

Observable low-resolution images

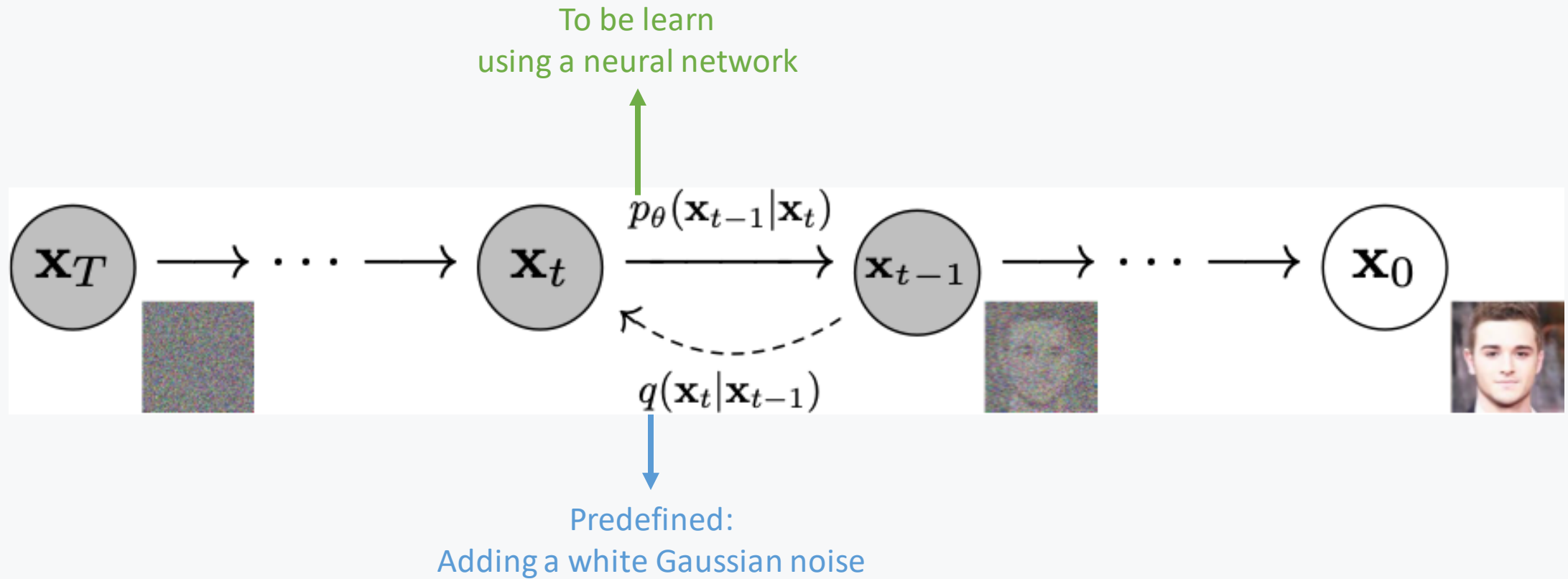


Generative diffusion model
→

A generated high-resolution image

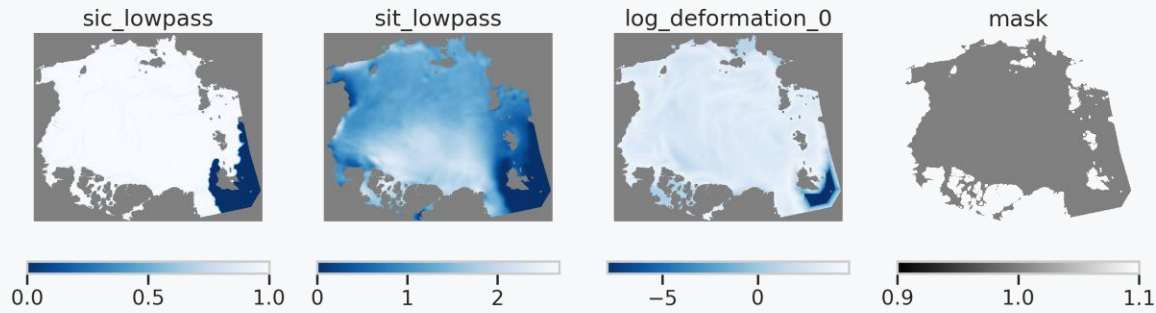


Principle of the diffusion model



Principle of the diffusion model in SuperIce

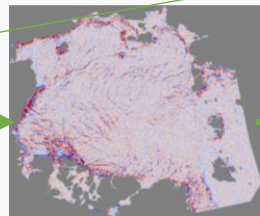
The low-resolution "context"
(low-resolution fields)



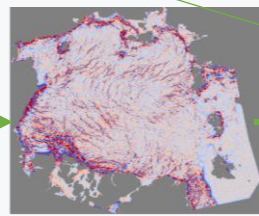
White gaussian noise



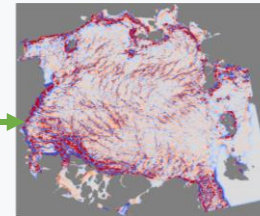
NN



NN

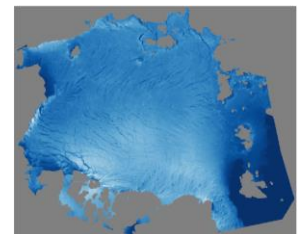
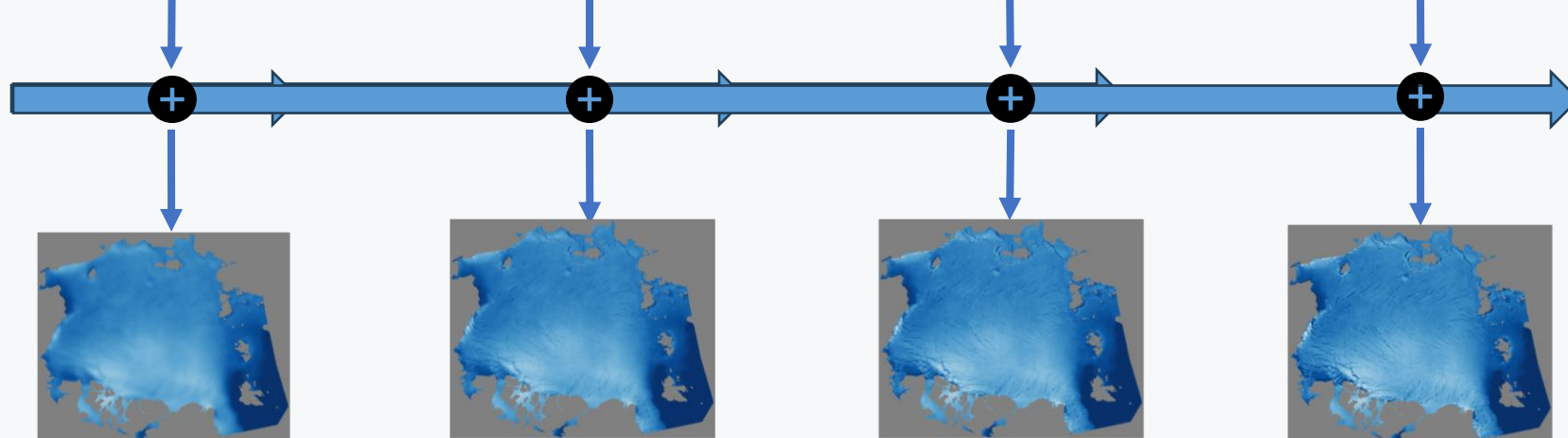
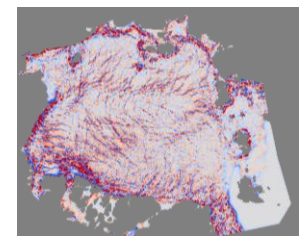


NN

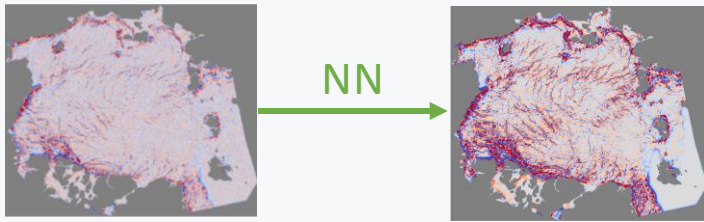


Generated image

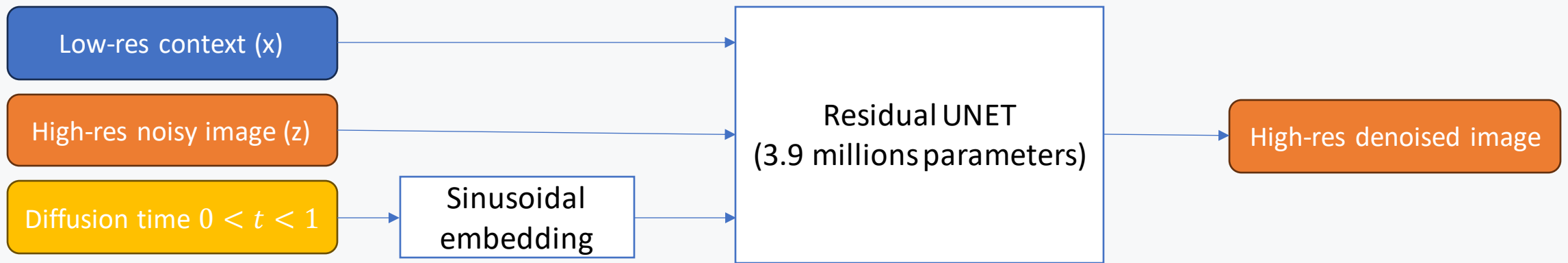
TARGET



Implementation details



Model Residual Neural network $f(x,z,t)$

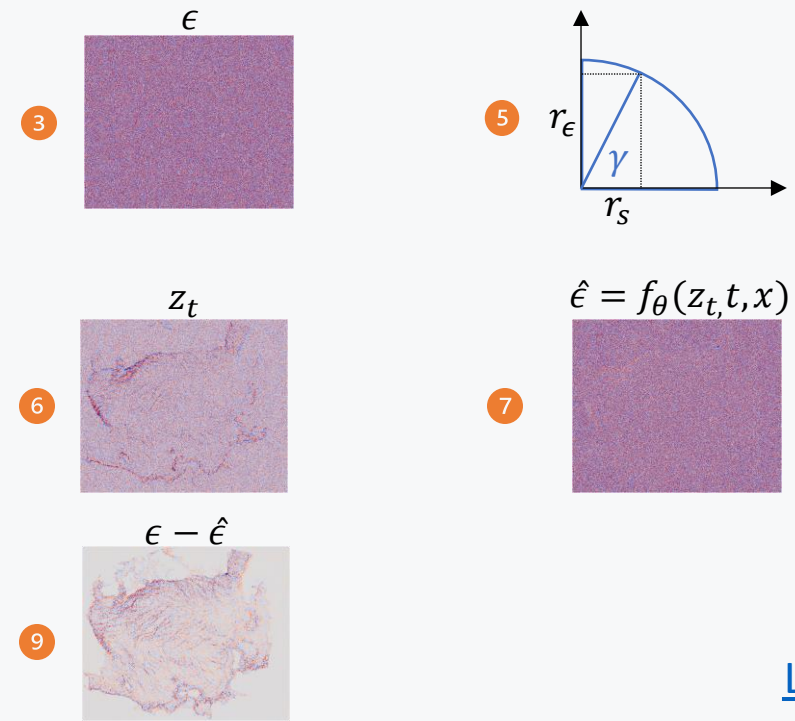


Training algorithm



For one sample

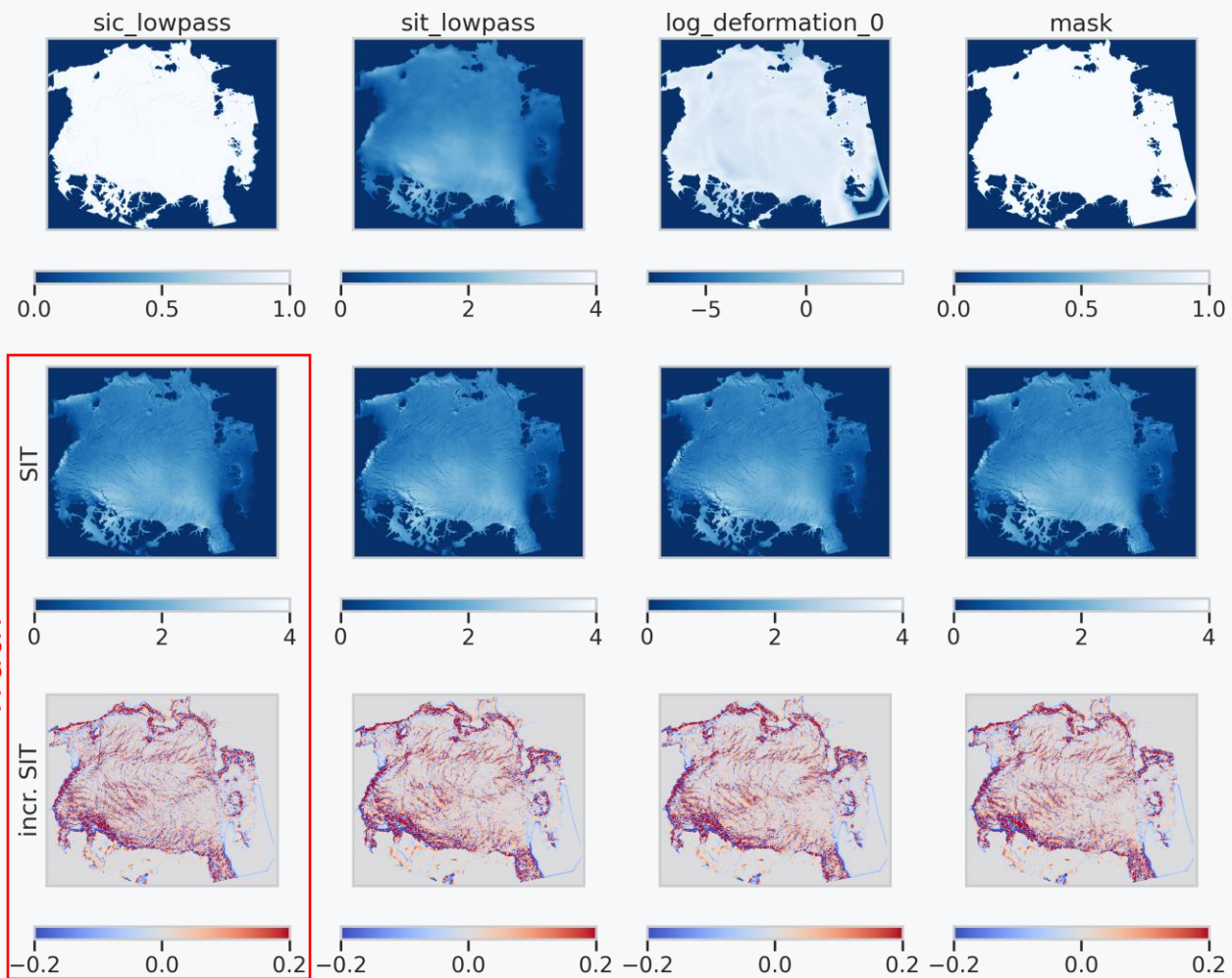
1. Draw a HR image y and a LR context x in the training set
2. Draw a diffusion time t between 0 (full signal) and 1 (full noise)
3. Draw a white Gaussian noise ϵ
4. Compute diffusion angle: $\gamma = \gamma_{min} + t \cdot (\gamma_{max} - \gamma_{min})$
5. Compute the signal and noise rate: $r_s = \cos \gamma$, $r_\epsilon = \sin \gamma$
6. Compute the noisy image: $z_t = r_s \cdot y + r_\epsilon \cdot \epsilon$
7. Predict the noise by the NN: $\hat{\epsilon} = f_\theta(z_t, t, x)$
8. Predict the image: $\hat{z}_{t-1} = (z_t - r_\epsilon \cdot \hat{\epsilon}) / r_s$
9. Compute the loss on the noise: $= L(\theta) = \|\epsilon - \hat{\epsilon}\|^2$
10. Minimize L



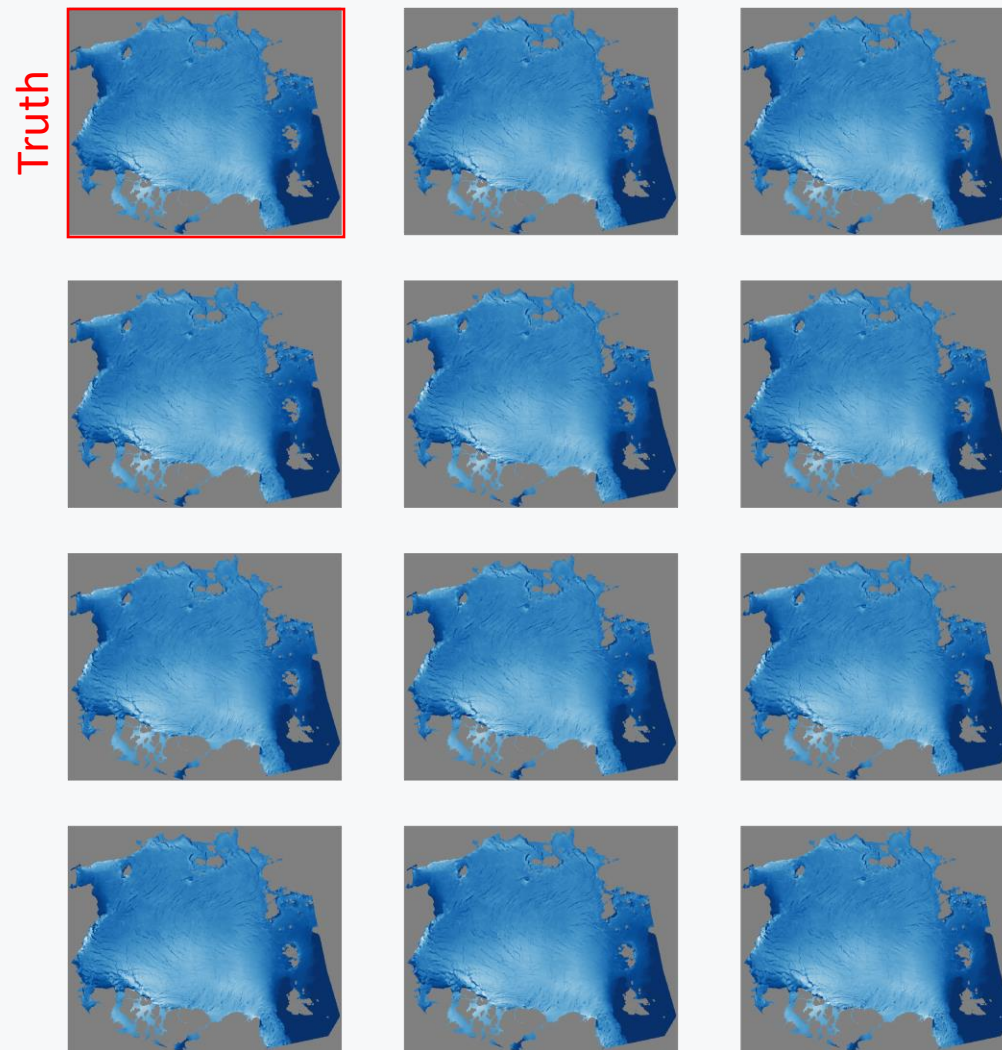
- ✓ Results of the 10 January 2021
- ✓ Results of the 23 October 2020
- ✓ Global results

Results of 26 January 2021

Generation of high-res SIT and residuals

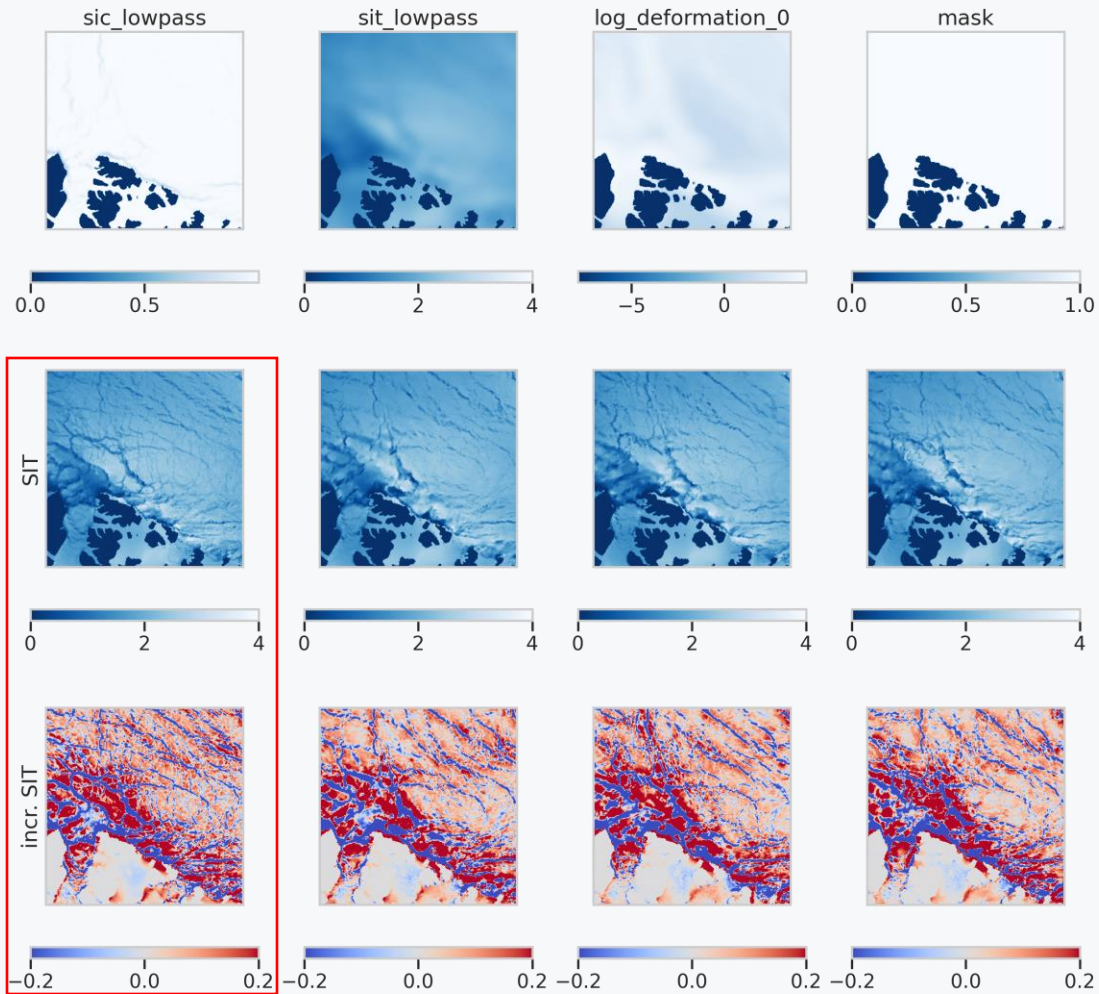


Generation of an ensemble

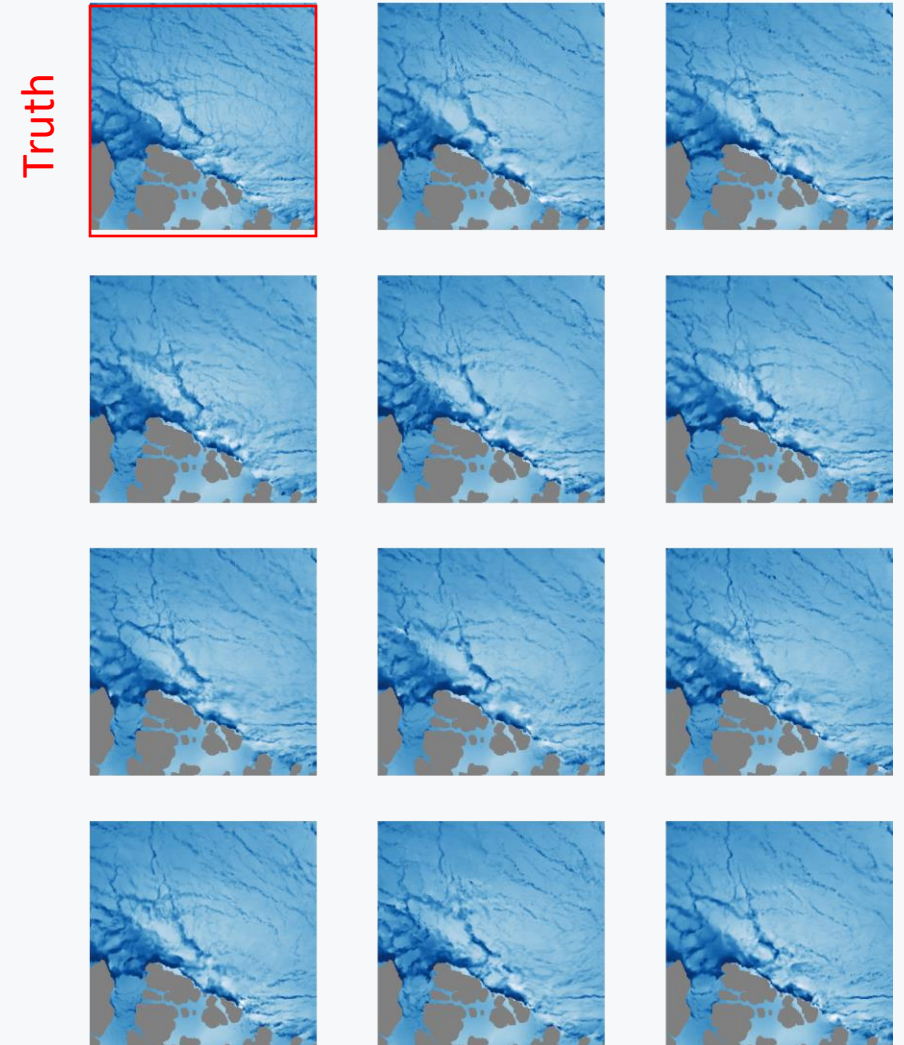


Results of 26 January 2021 (zoom)

Generation of high-res SIT and residuals

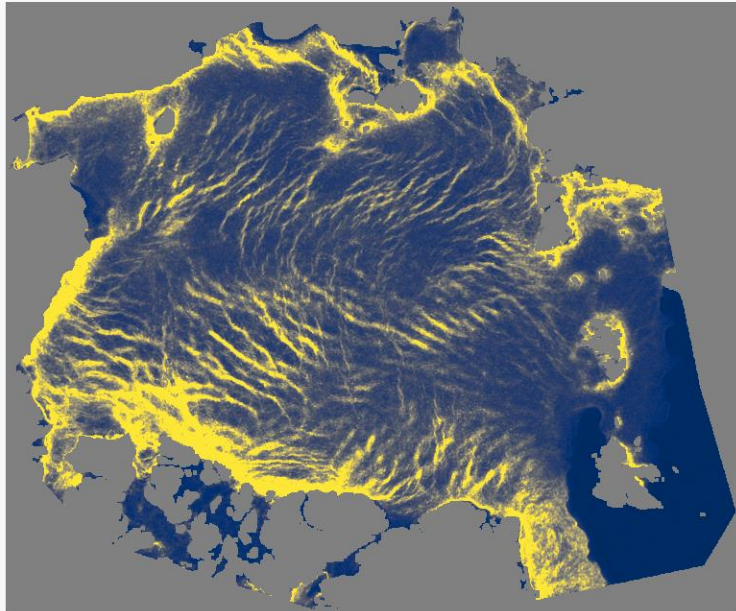


Generation of an ensemble

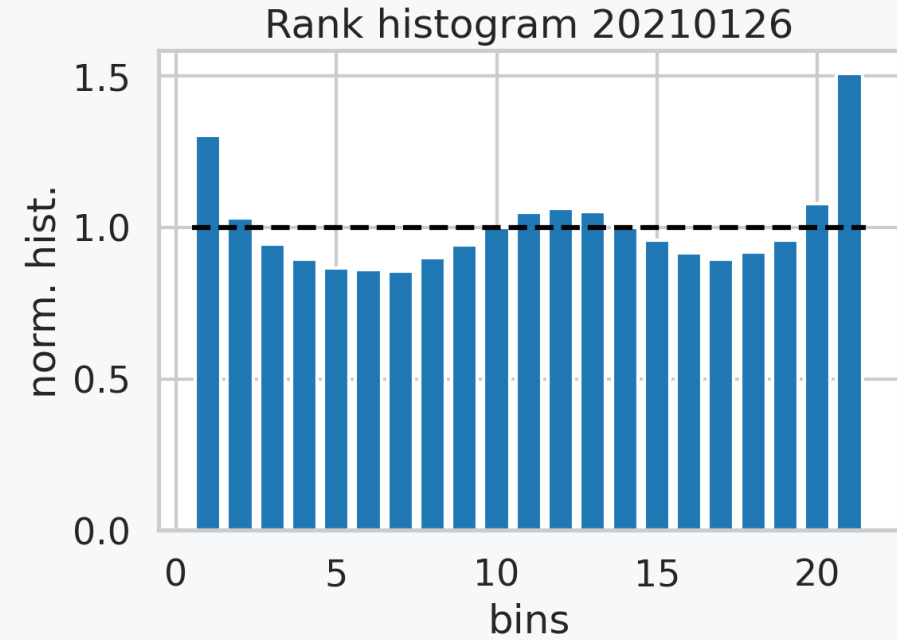
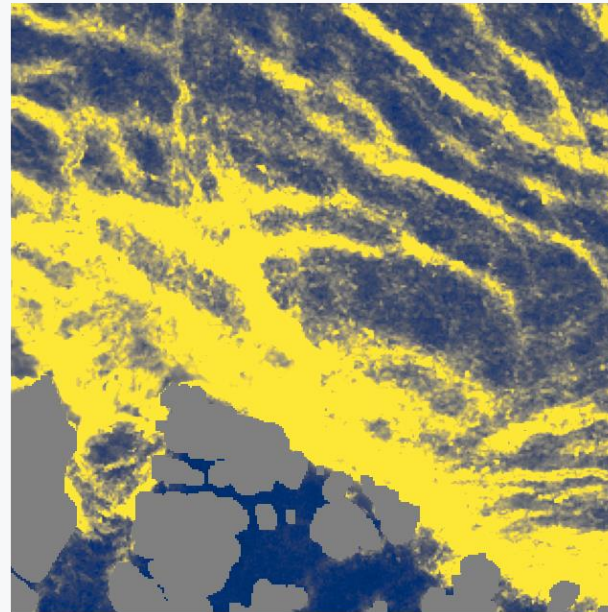


Results of 26 January 2021

Spread and reliability



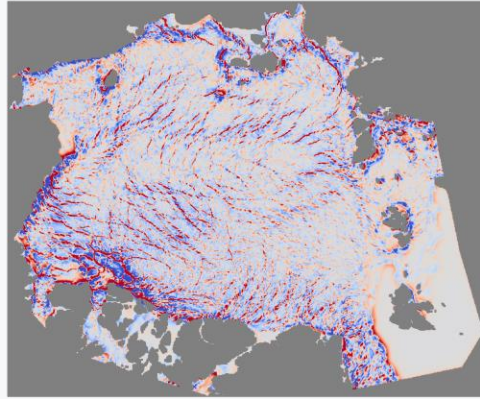
zoom



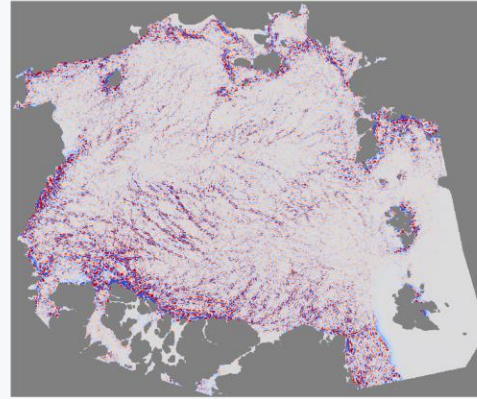
Results of 26 January 2021

Accuracy

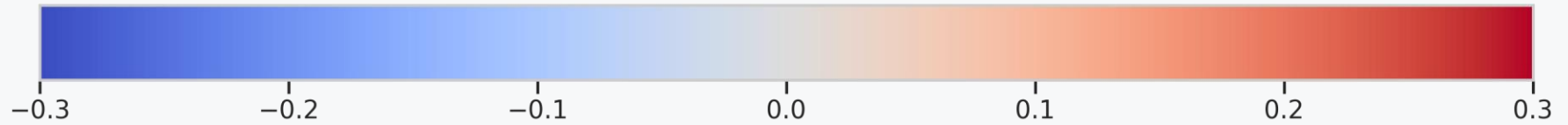
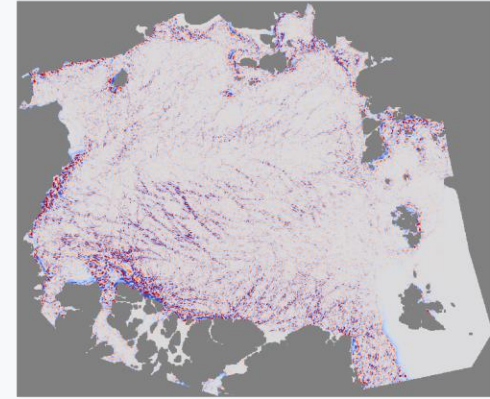
LR error 1.69e-01



member error 1.62e-01

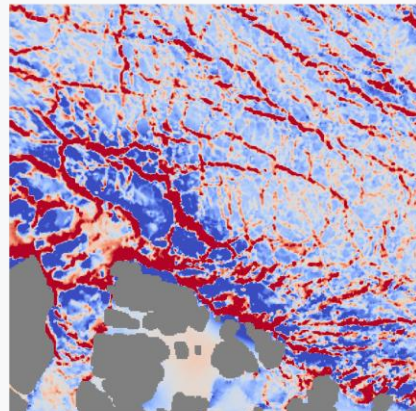


average error 1.19e-01

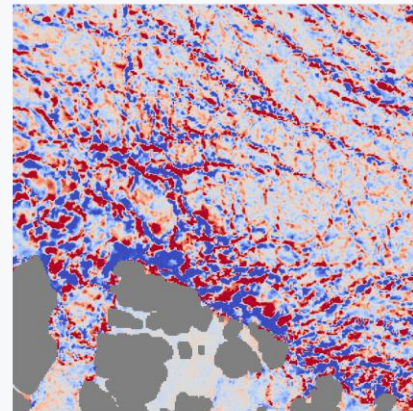


zoom

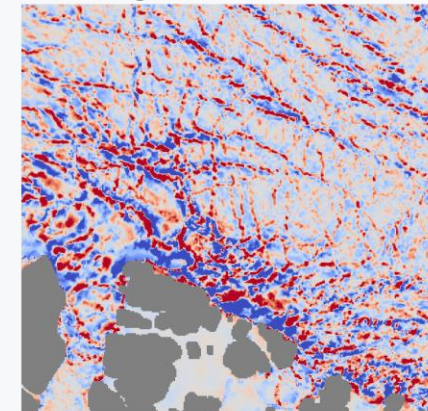
LR error 2.79e-01



member error 2.64e-01

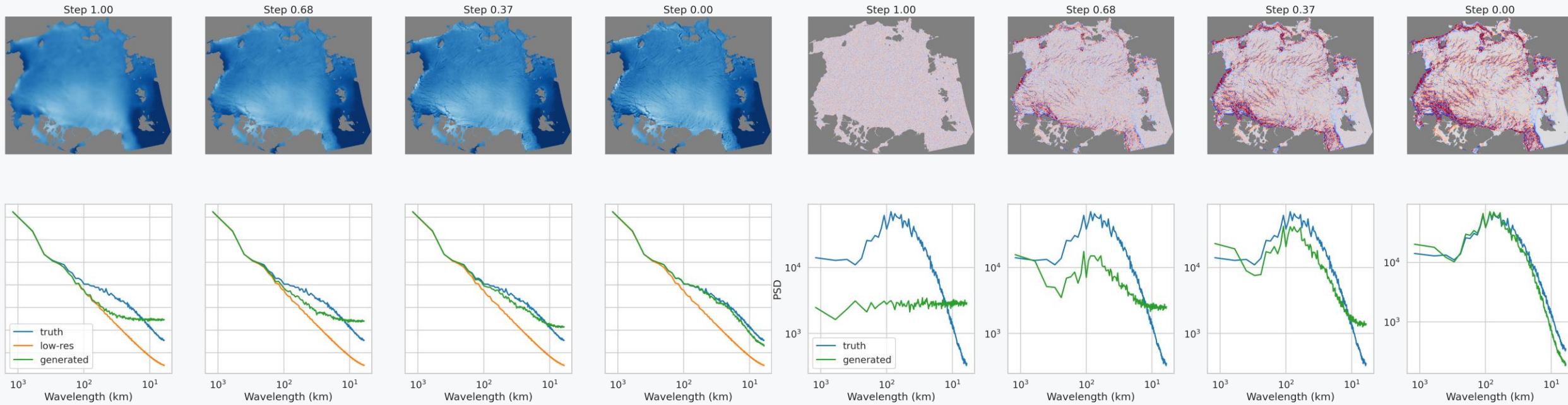


average error 1.99e-01



Spectrum 26 January 2021

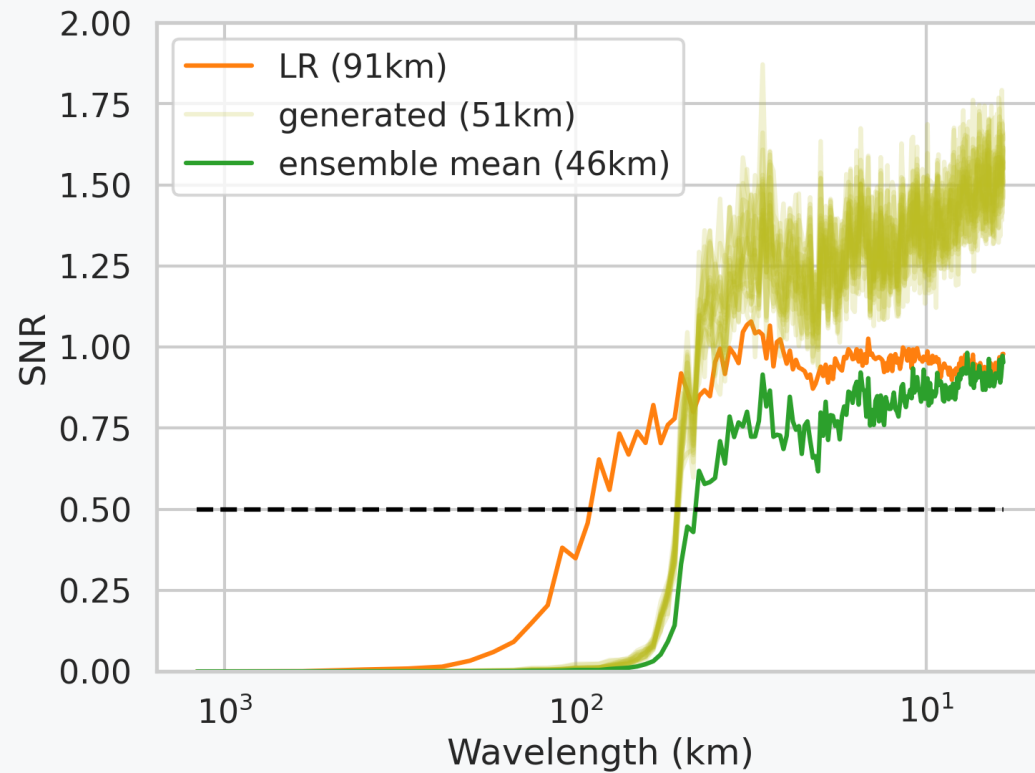
Power Spectrum Density as a function of the diffusion time (Step)



Spectrum

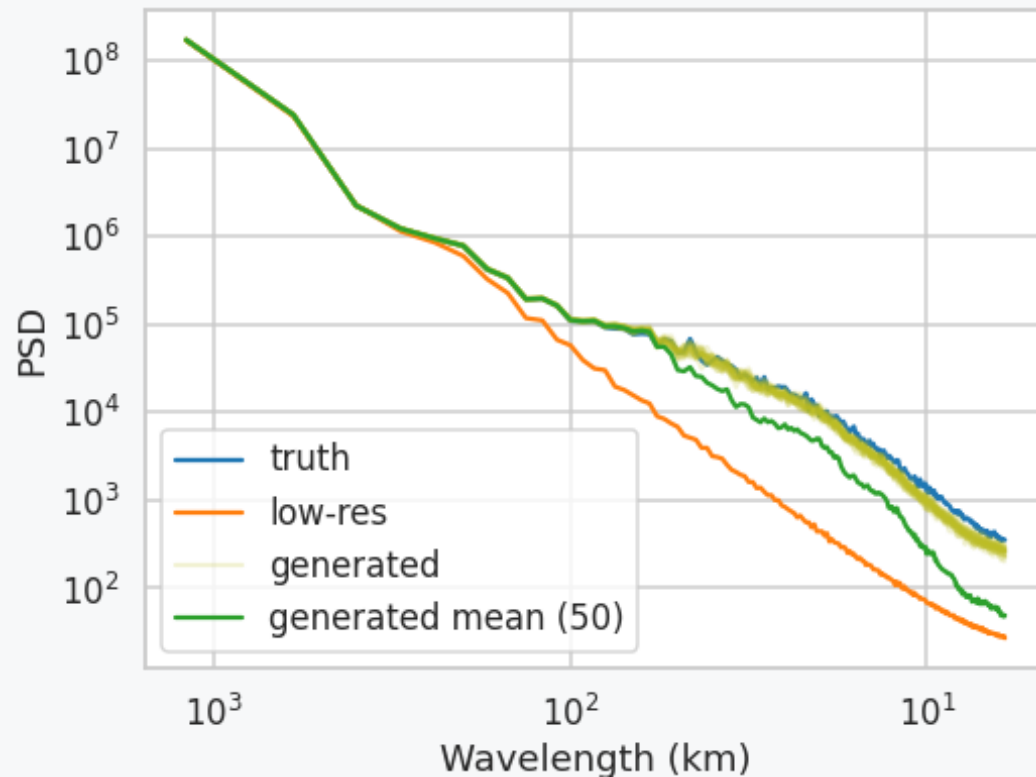
Signal to noise

Spectral ratio = $\text{PSD}(\text{reconstruction-truth}) / \text{PSD}(\text{truth})$

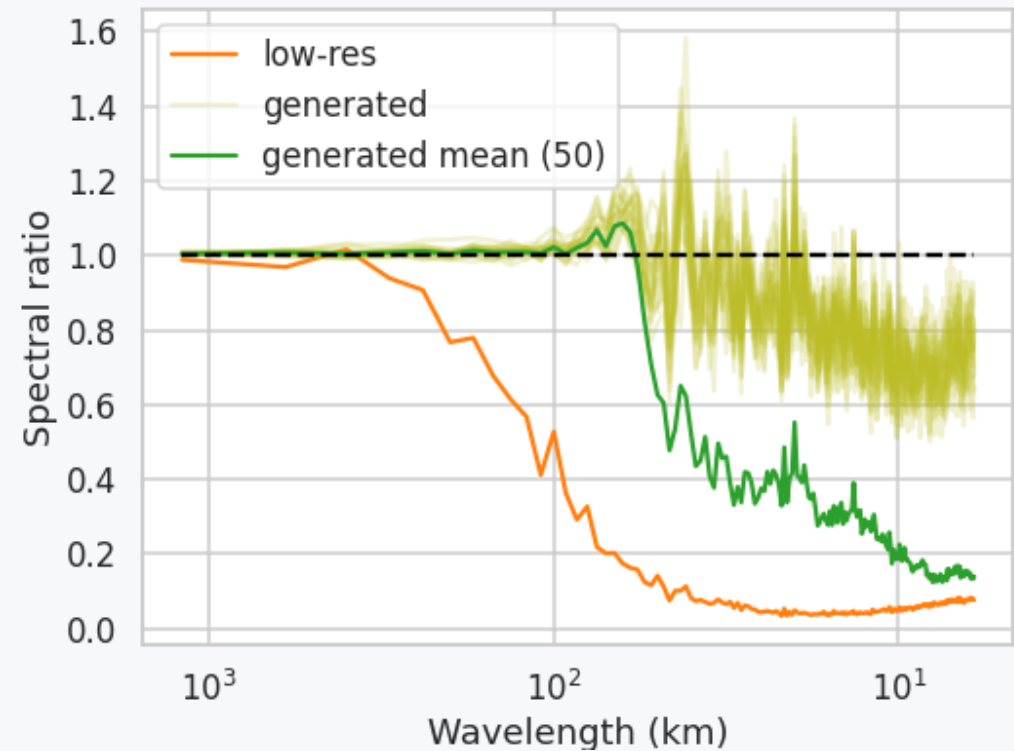


Spectrum

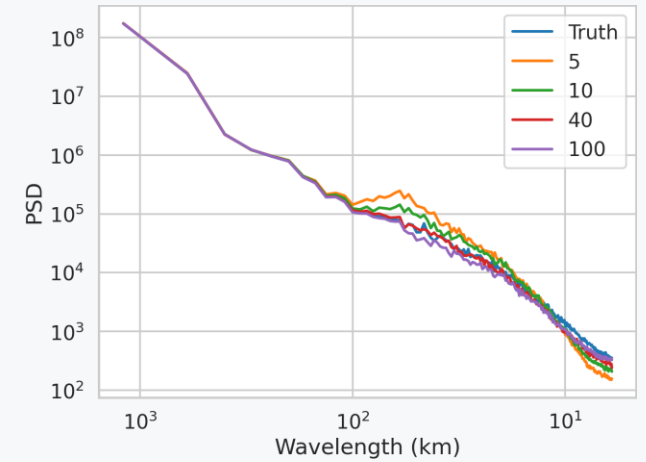
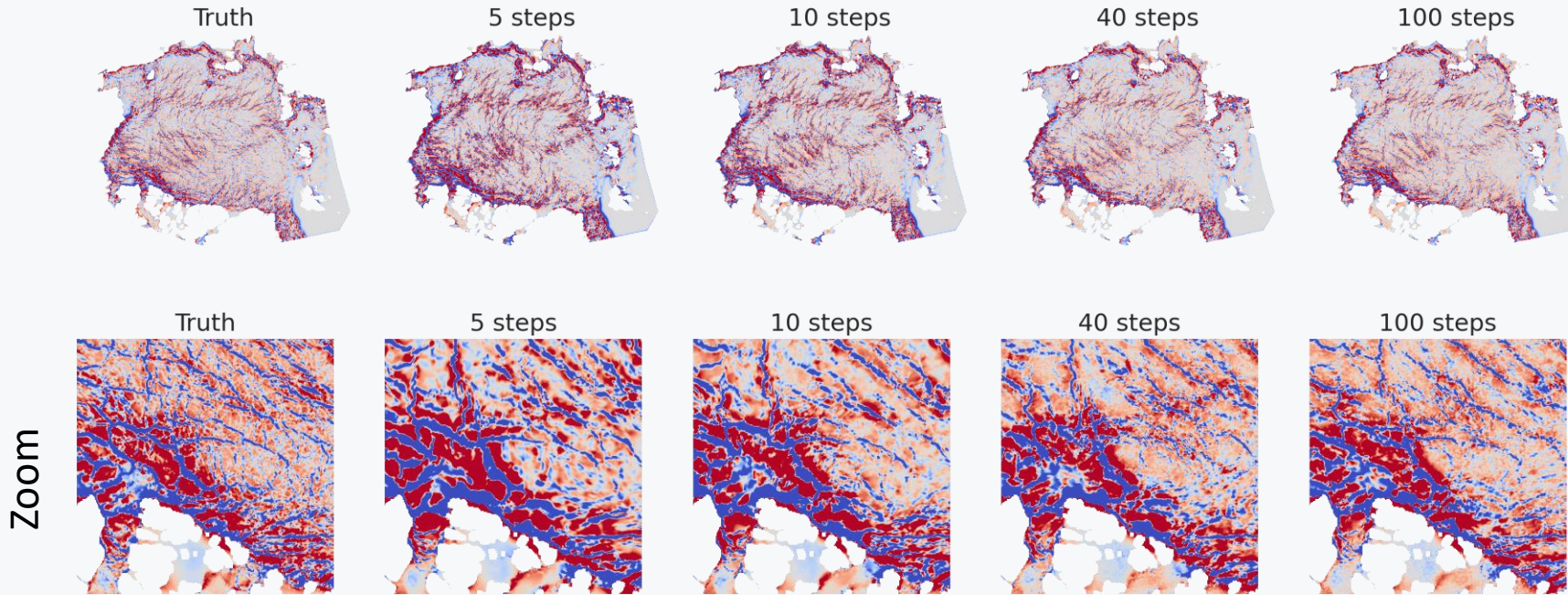
Power Spectrum Density



Spectral ratio = PSD-reconstruction / PSD-truth



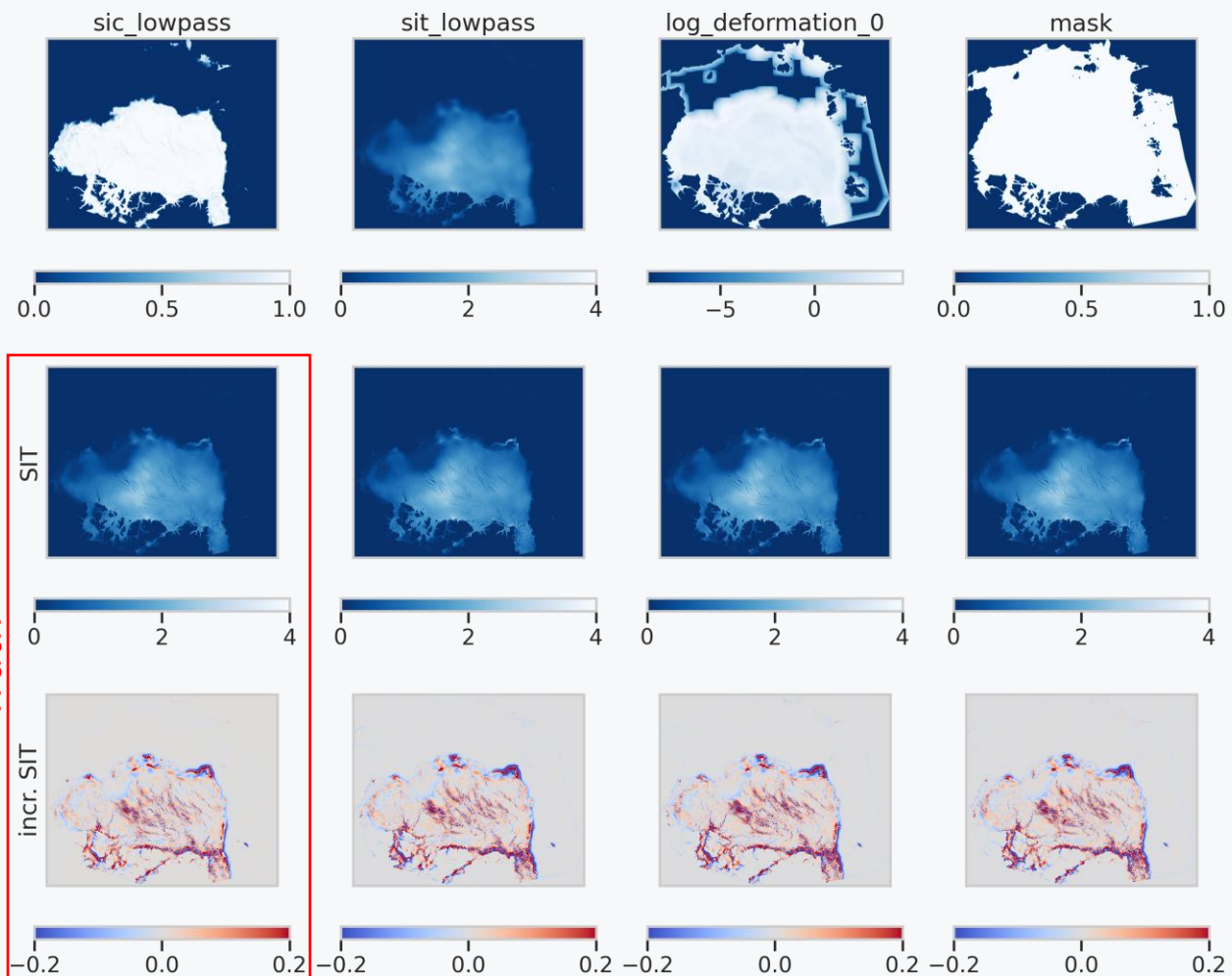
Sensitivity to the number of diffusion steps



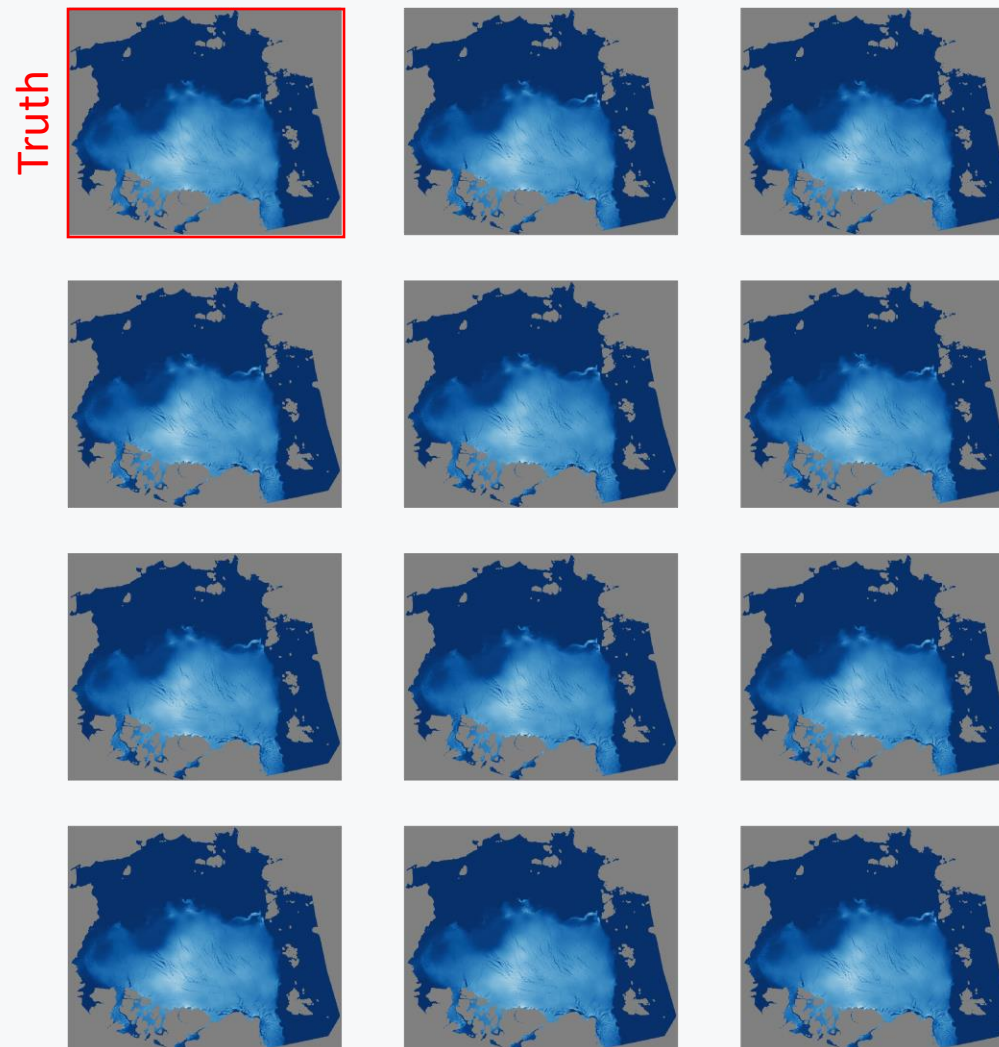
In the other sections, 40 steps are used

Results of 23 October 2020

Generation of high-res SIT and residuals

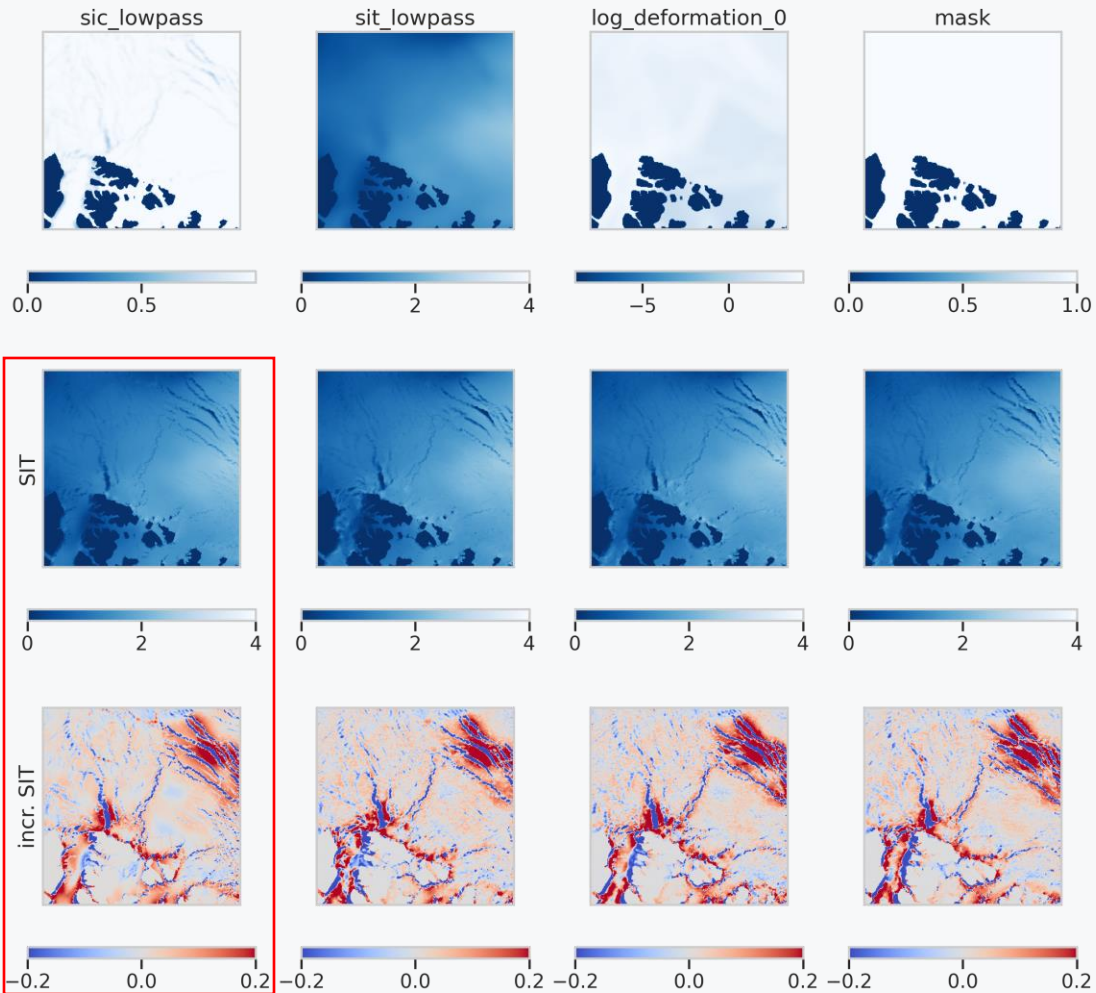


Generation of an ensemble

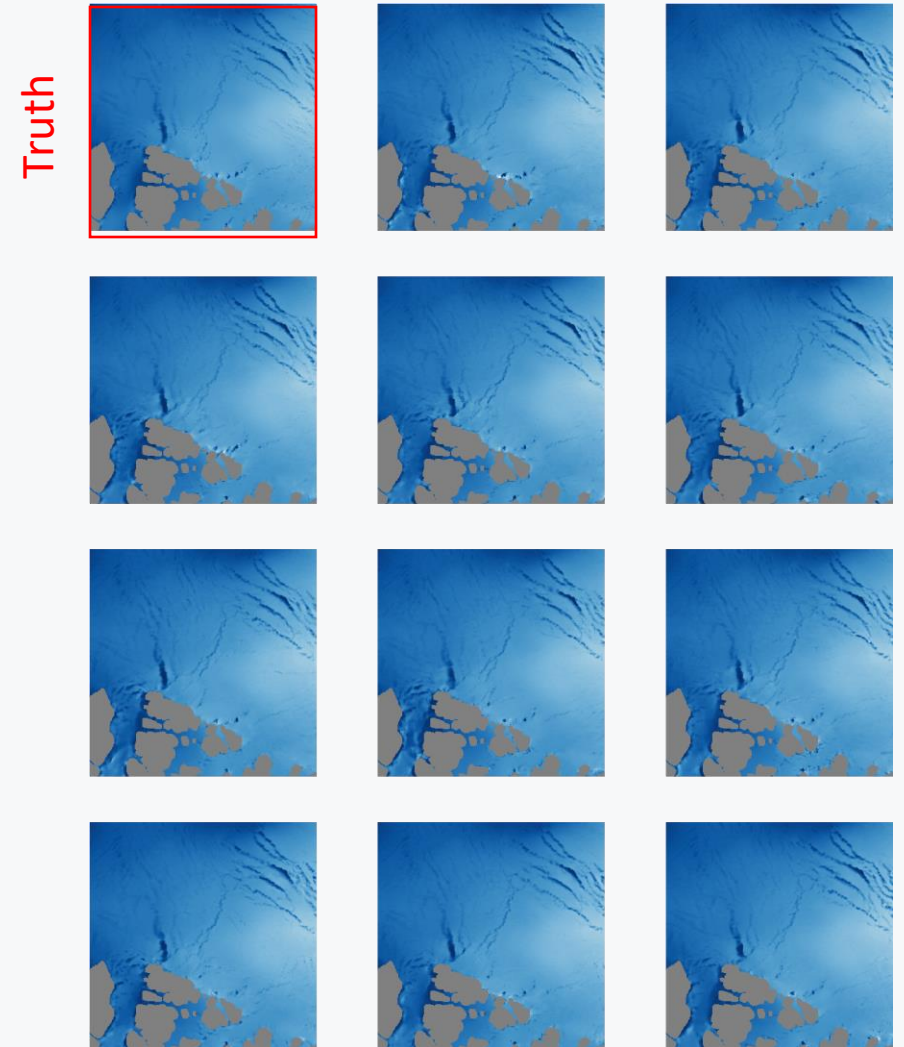


Results of 23 October 2020 (zoom)

Generation of high-res SIT and residuals

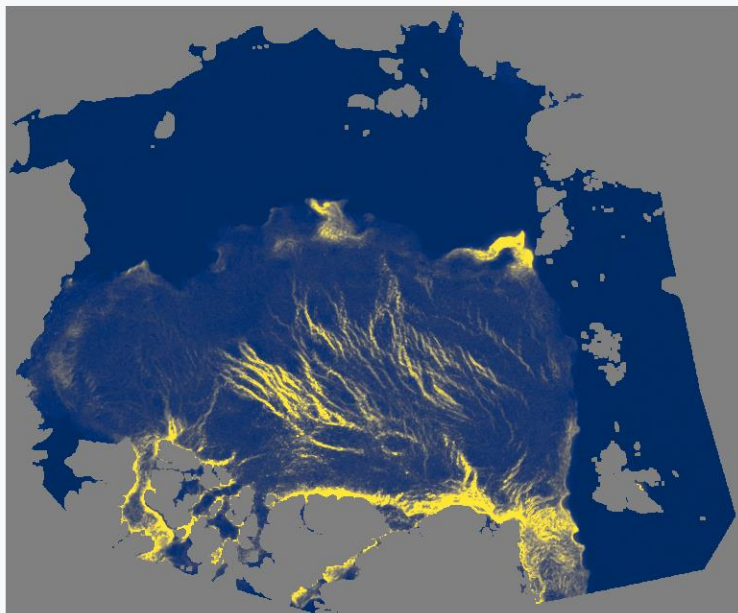


Generation of an ensemble

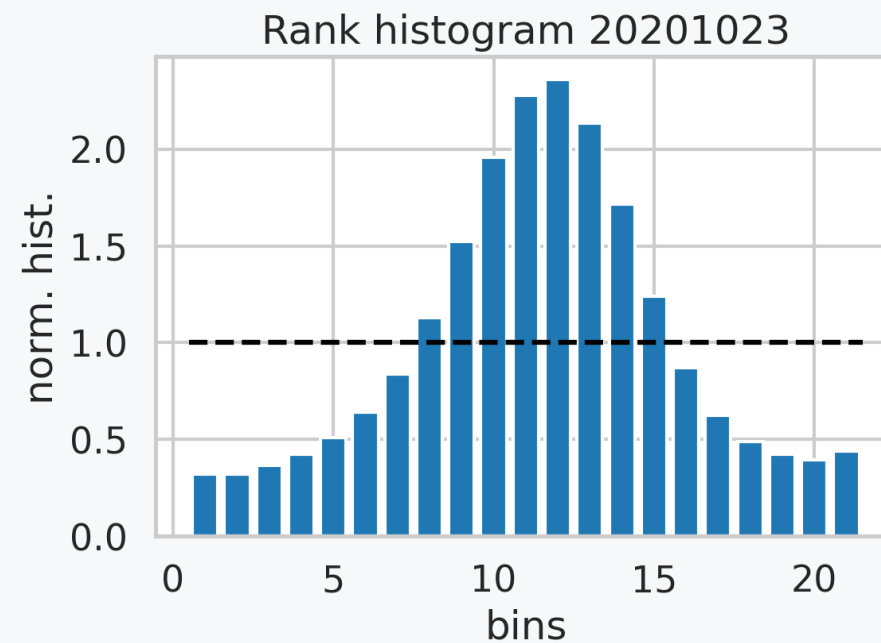
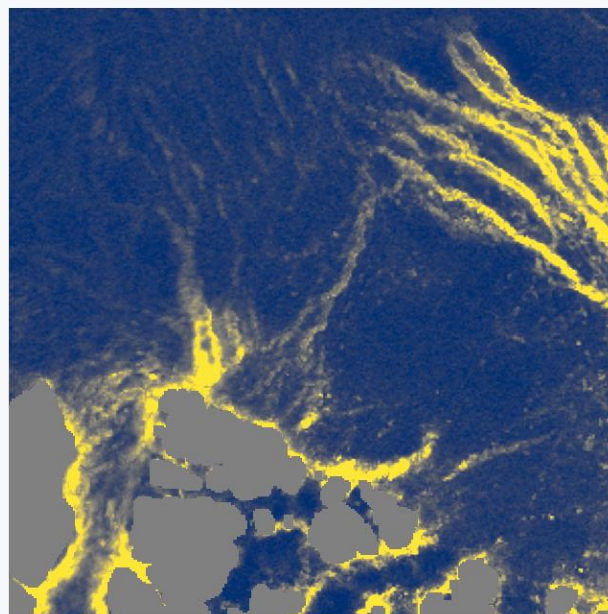


Results of 23 October 2020

Spread and reliability



zoom



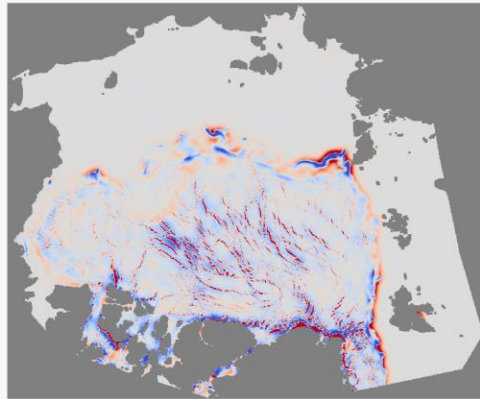
Ensemble over-dispersive



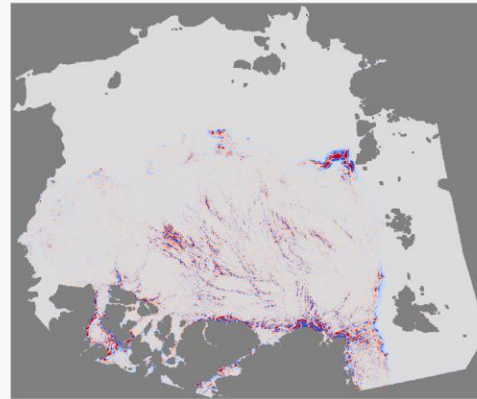
Results of 23 October 2020

Accuracy

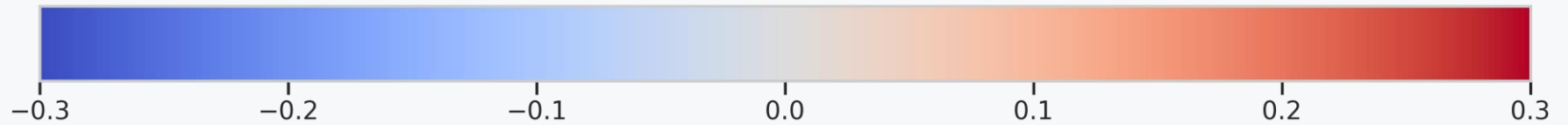
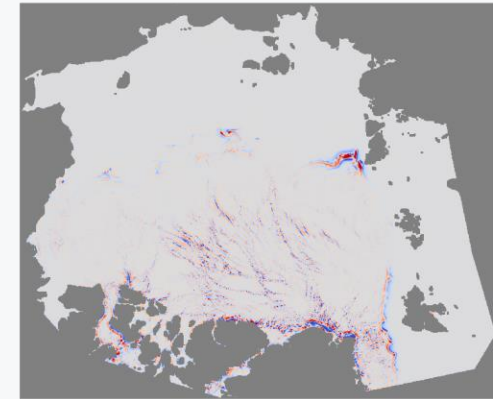
LR error $9.59e-02$



member error $8.52e-02$

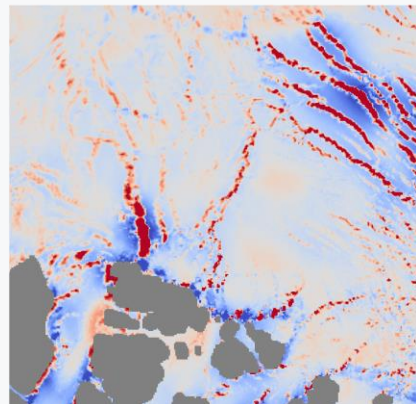


average error $5.75e-02$

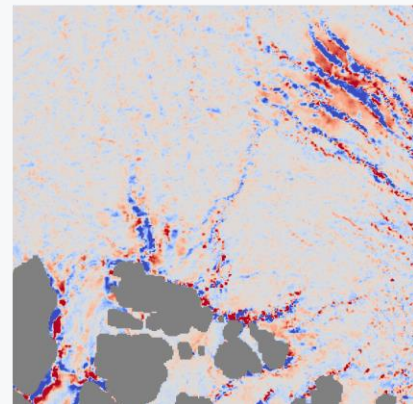


zoom

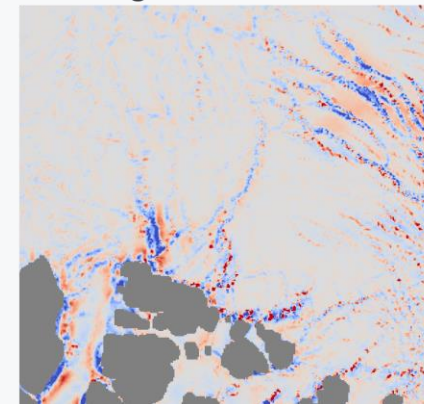
LR error $1.32e-01$



member error $1.22e-01$

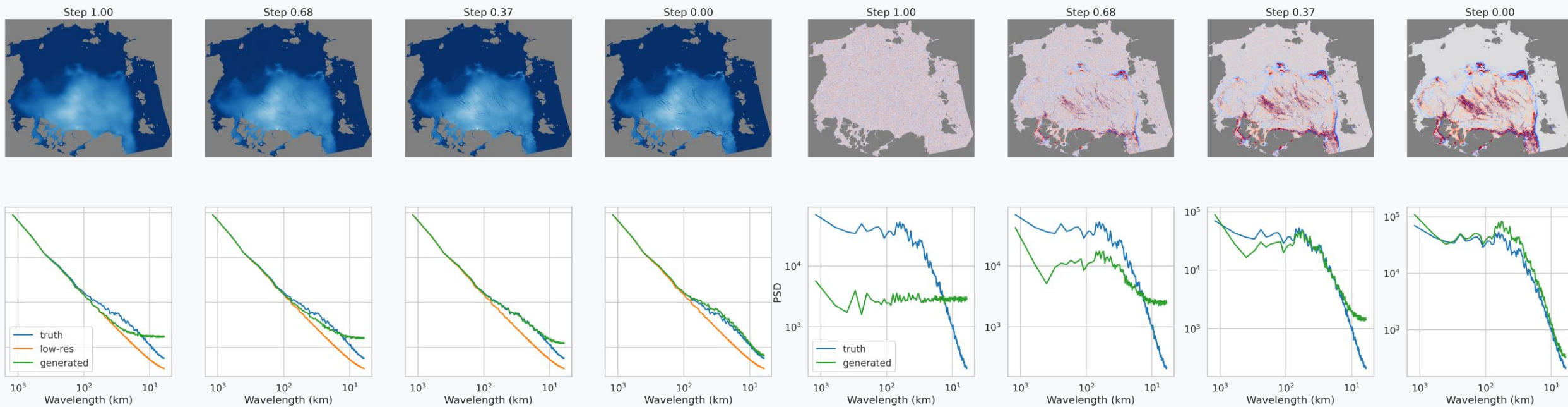


average error $7.66e-02$



Spectrum 23 October 2020

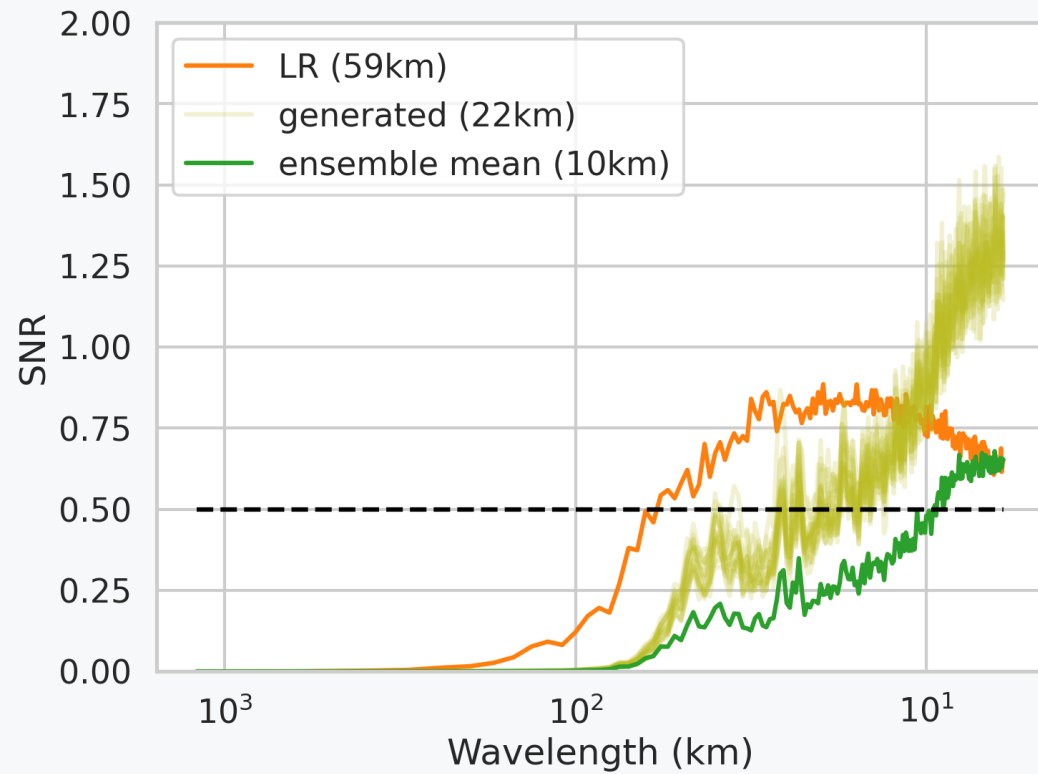
Power Spectrum Density as a function of the diffusion time (Step)



Spectrum

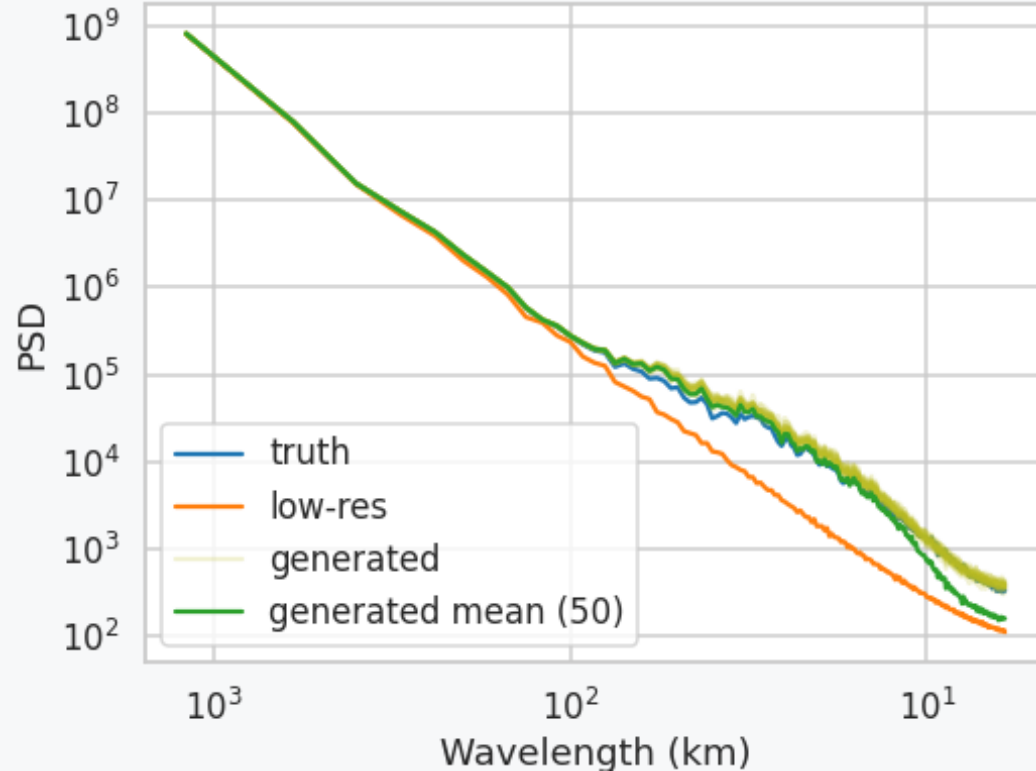
Signal to noise

Spectral ratio = $\text{PSD}(\text{reconstruction-truth}) / \text{PSD}(\text{truth})$

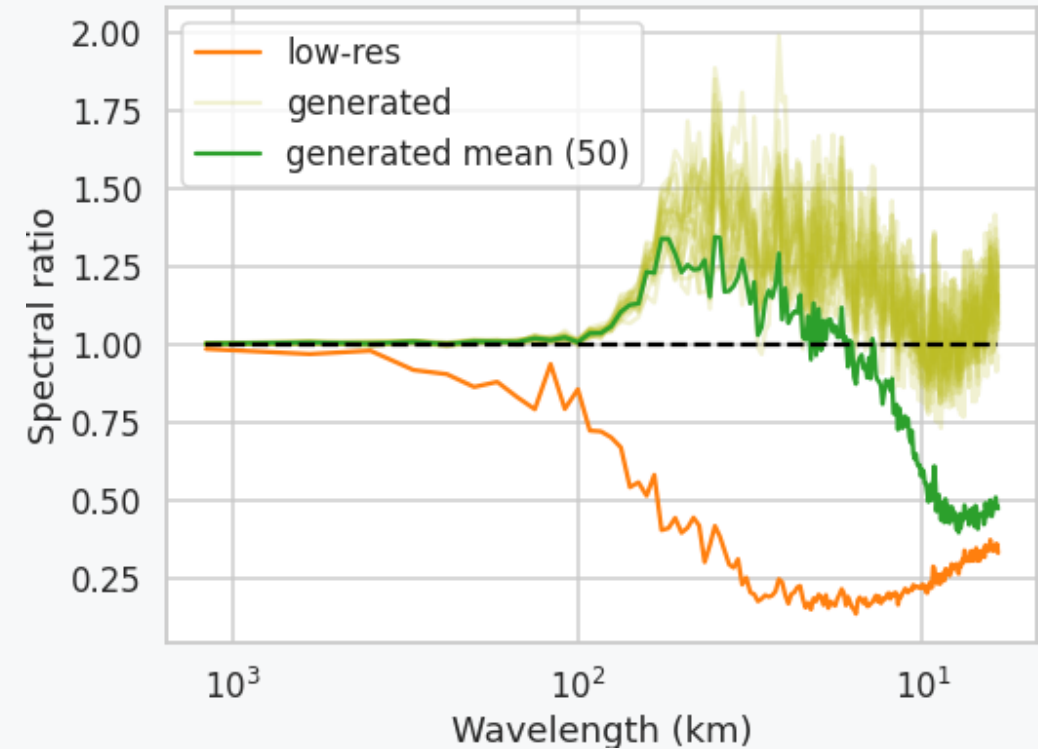


Spectrum

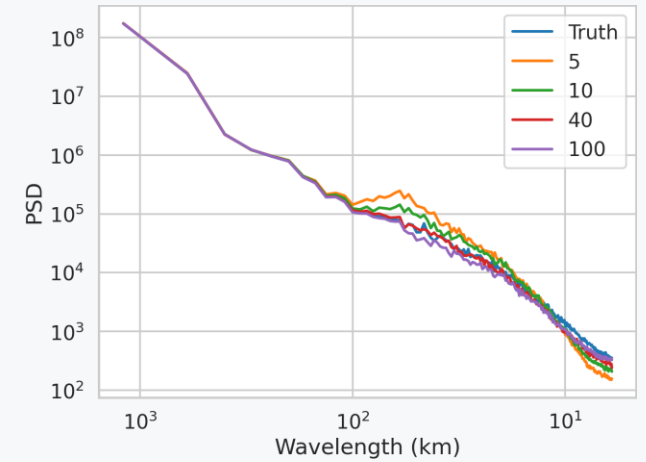
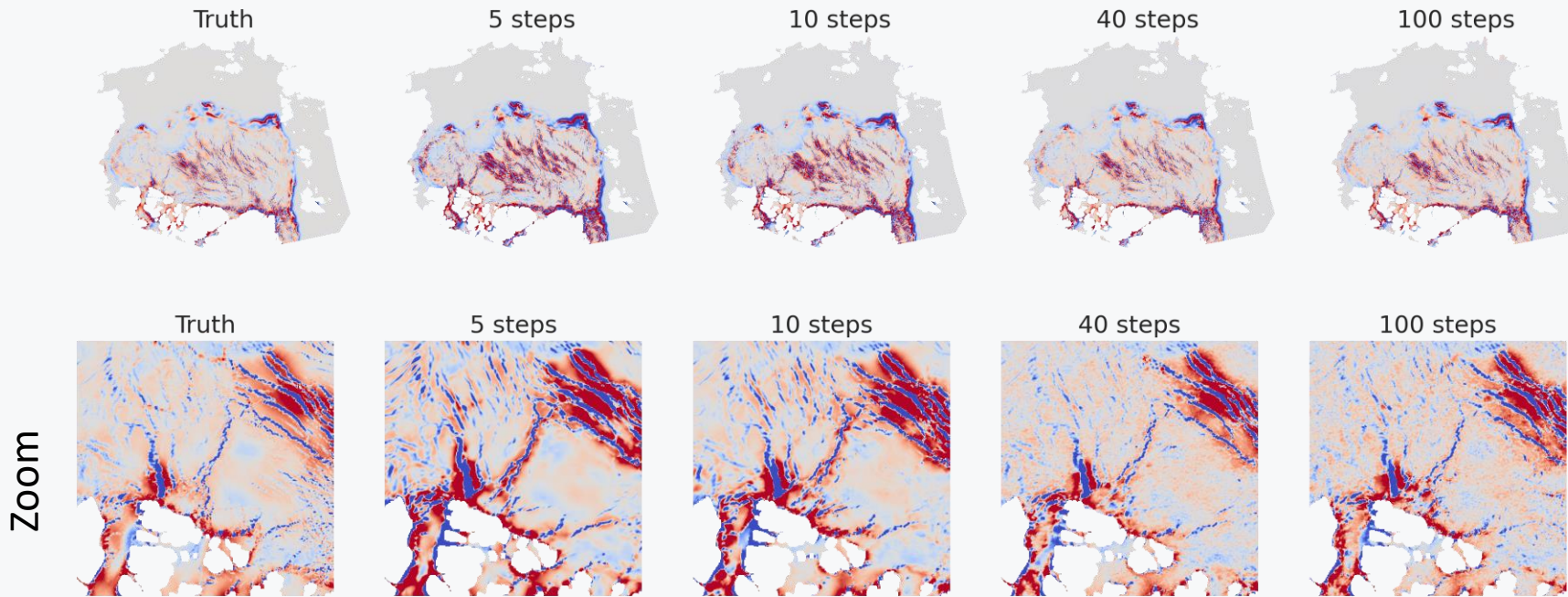
Power Spectrum Density



Spectral ratio = PSD-reconstruction / PSD-truth



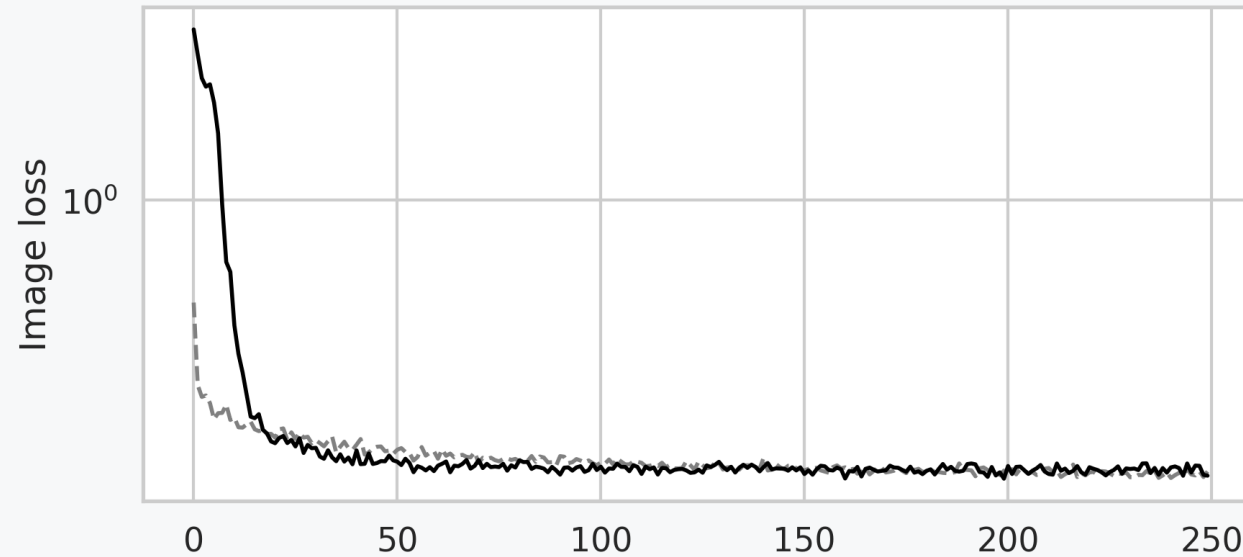
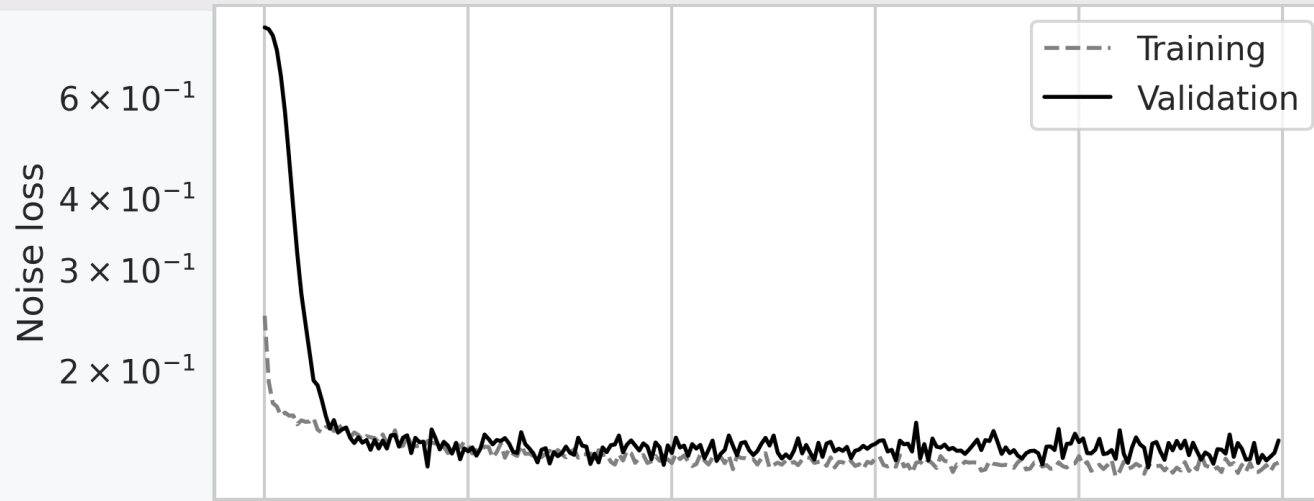
Sensitivity to the number of diffusion steps



In the other sections, 40 steps are used

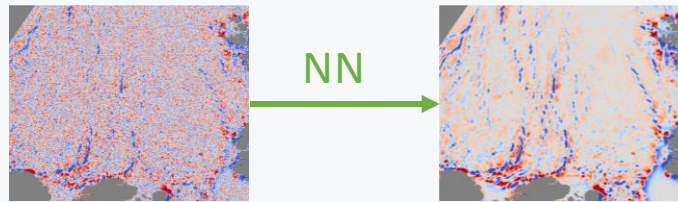
Globals results

Learning curve

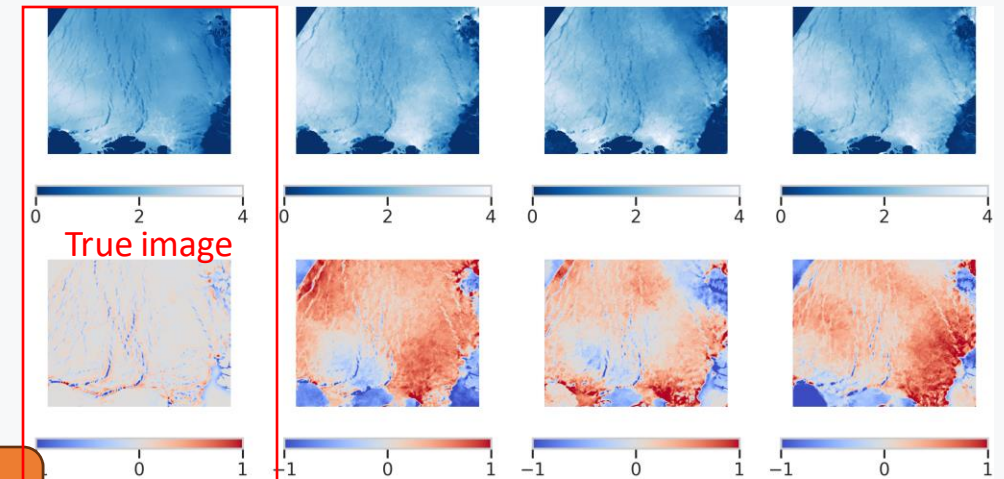
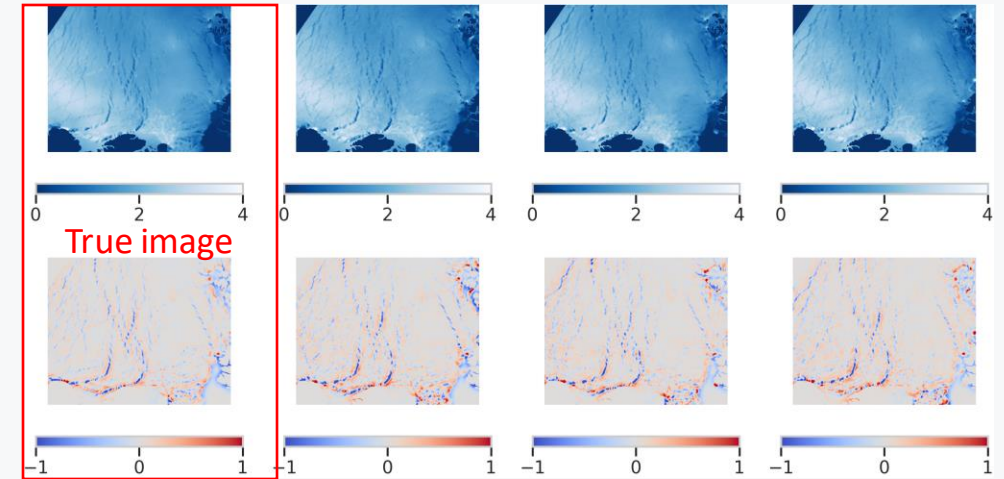


Residual Vs full field generation

Residual generation



Full-field generation



Full-field induces large-scale biases