

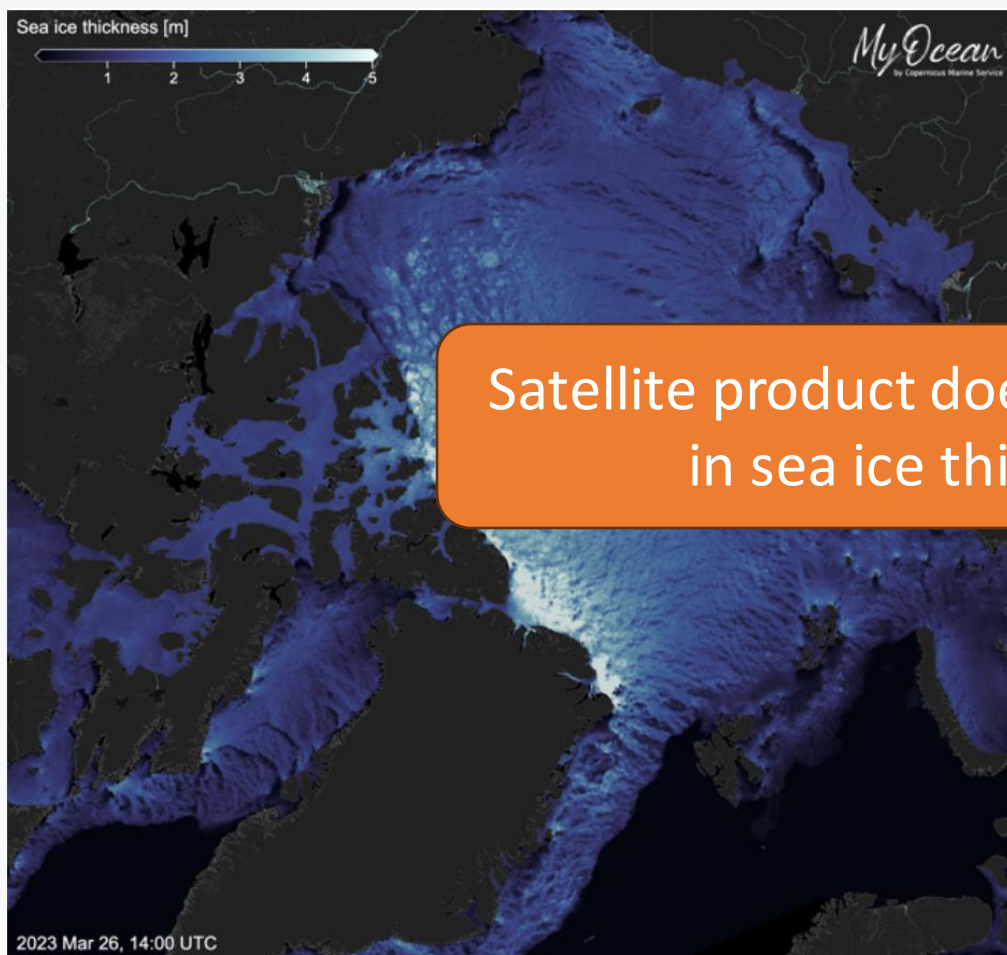
Super-resolution of sea ice thickness using diffusion models

Julien Brajard, Anton Korosov, Yiguo Wang, Richard Davy



Motivation

Physical model (NeXtSIM) forecast



Satellite observation product (CS2SMOS)



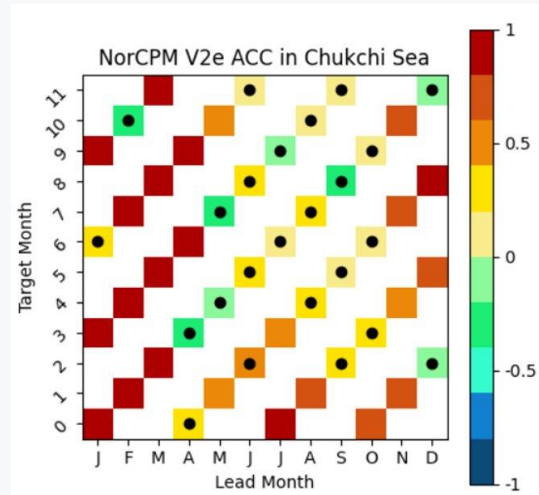
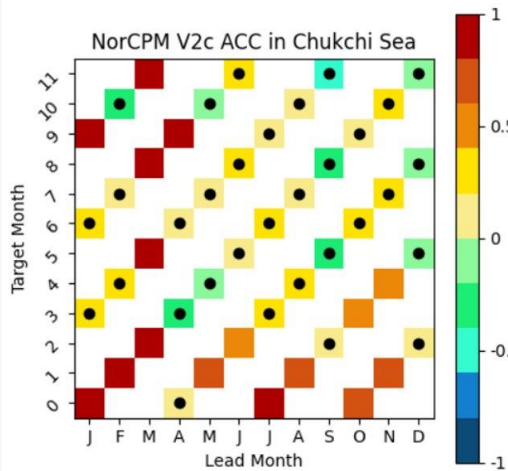
Satellite product does not resolve small scales in sea ice thickness (e.g. leads)

Why is it important?

Case 1: Predictability

Forecast skill

Detrended correlation coefficient of Sea ice extent in Chukchi Sea



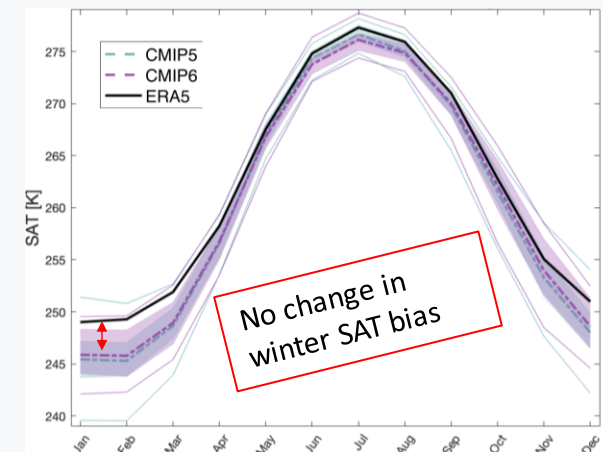
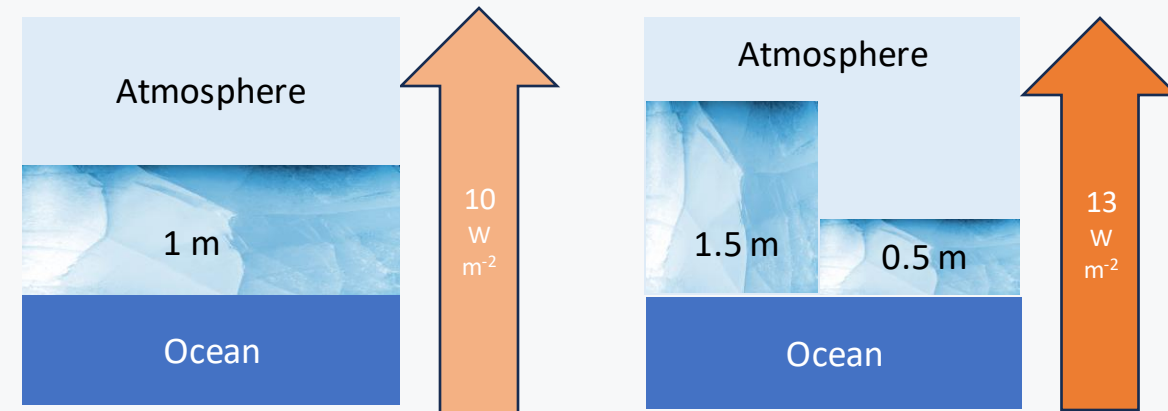
Initialization using Sea ice concentration observations only

Initialization using Sea ice concentration observations + Sea ice thickness only

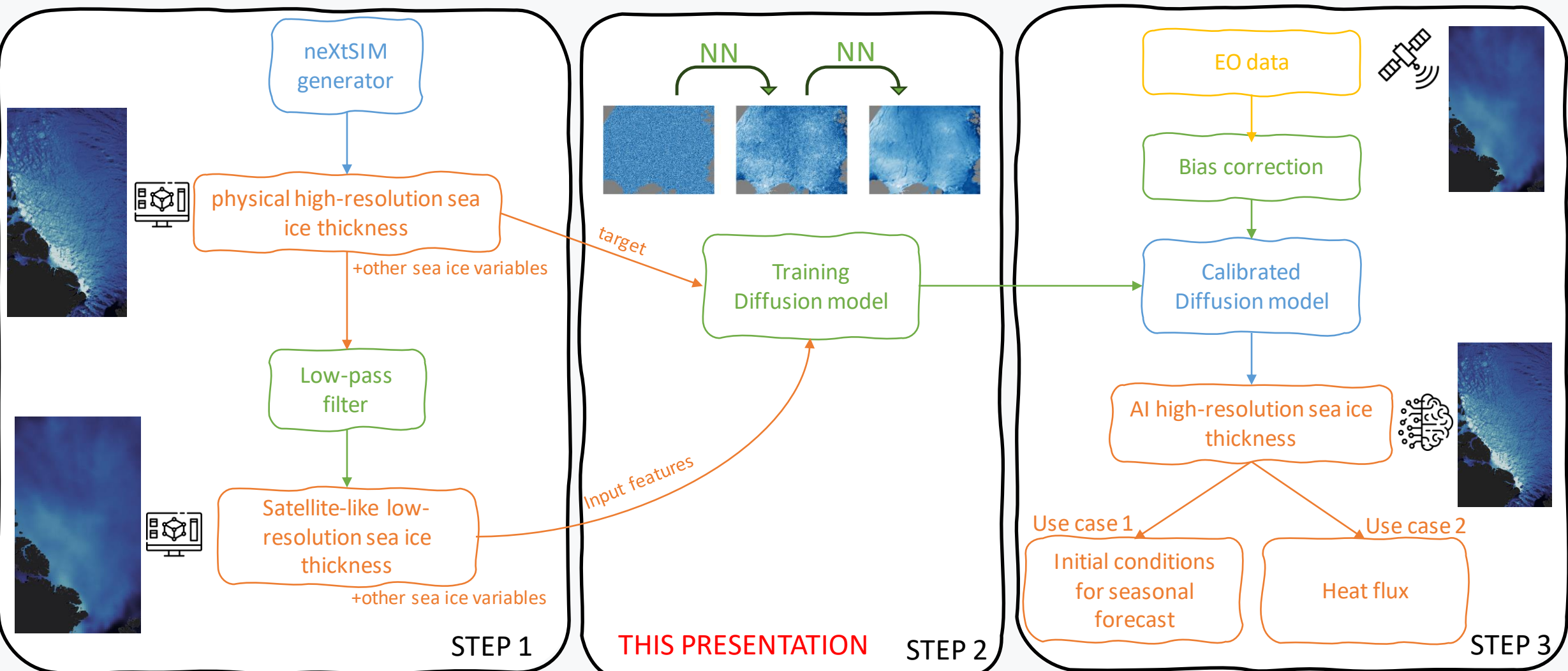
Black dot means not significant

Courtesy of N. Williams

Case 2: Surface fluxes



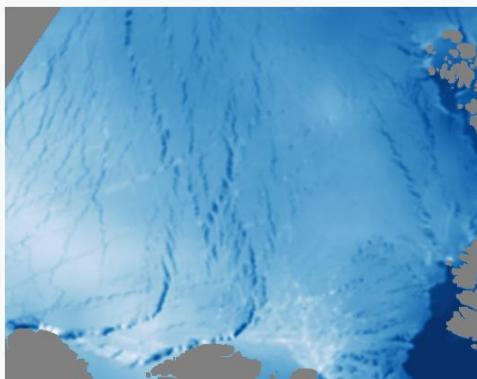
Steps of the project



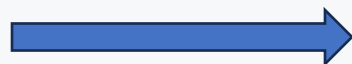
Step 1: Dataset constitution

Principle: Filtering of NeXtSIM simulations

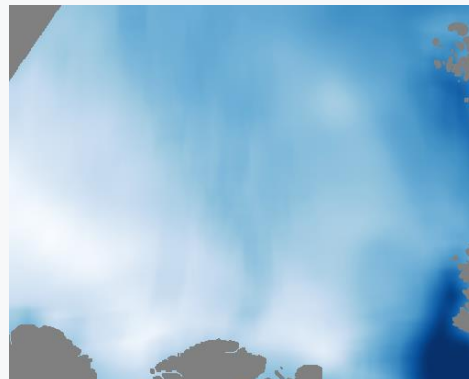
NeXtSIM sea ice thickness
11-01-2020 (res 4km)



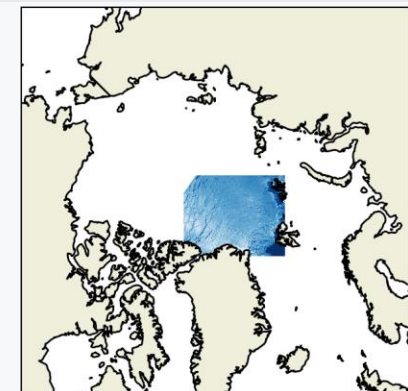
Convolution constant
kernel (size 120 km)



Filtered sea ice thickness
(res ~ 120 km)

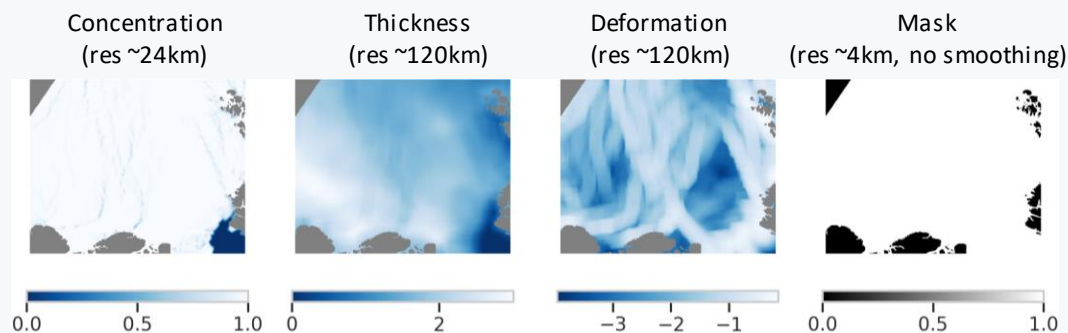


Observation product (CS2SMOS)
11-01-2021



Dataset:

- 4 input features (filtered)
- 529 samples, from 01-01-2020 to 30-09-2020
- Training: 10-10 -> 20-09 (509 samples)
- Validation 04-10-> 09-10 and 21-09->26-09 (12 samples)

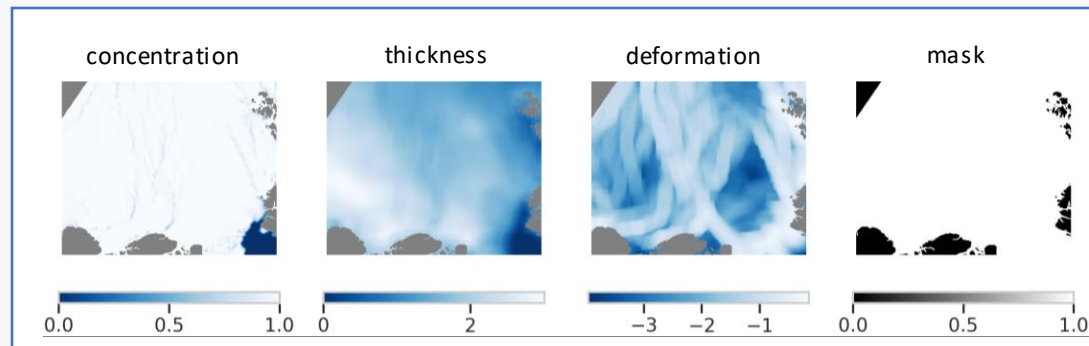


Apply diffusion model to sea ice thickness super-resolution

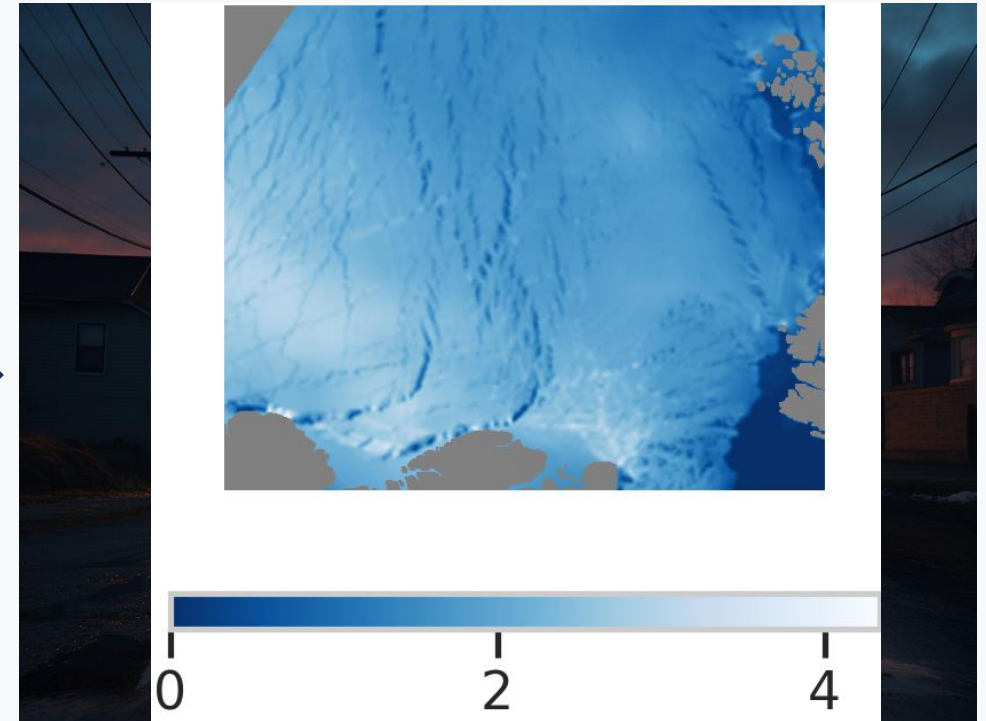
Used for AI image generator (Ex: Midjourney)

Observable low-resolution images

A generated high-resolution image

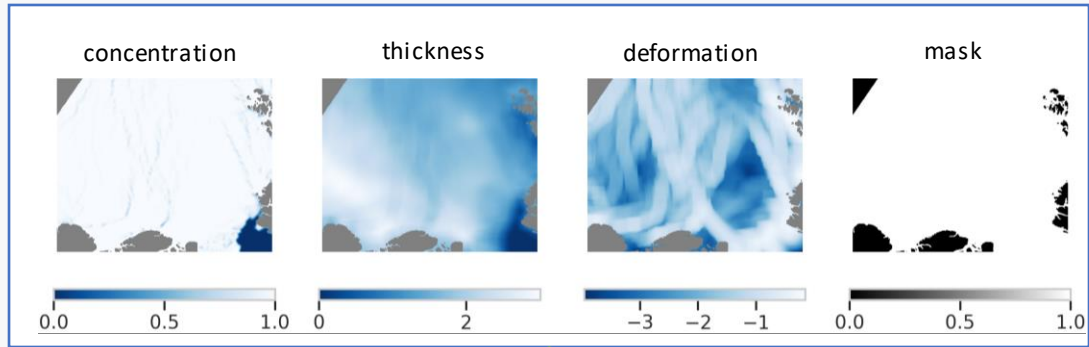


Generative
diffusion model

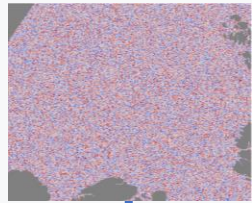


Principle of the diffusion model

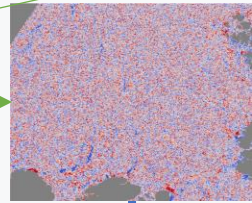
The low-resolution "context"
(low-resolution fields)



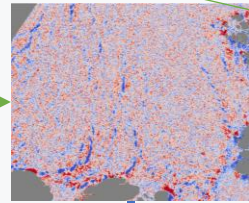
White gaussian noise



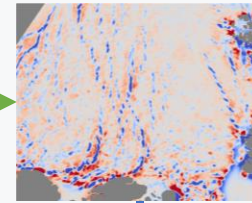
NN



NN



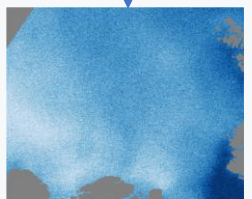
NN



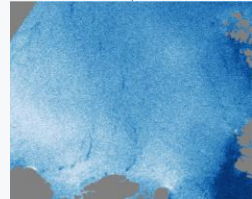
Generated image



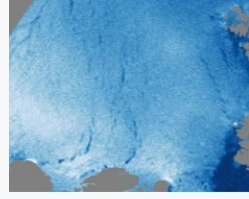
+



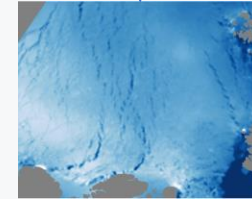
+



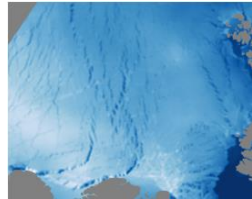
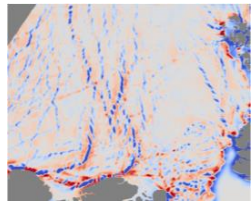
+



+



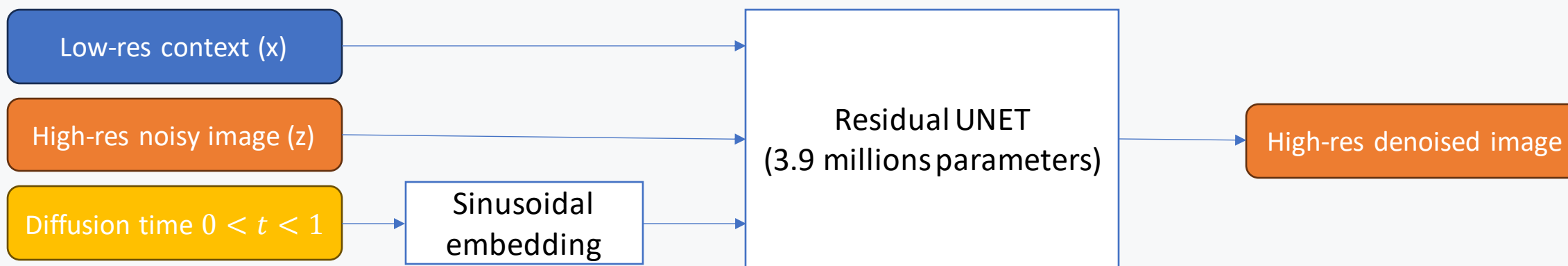
TARGET



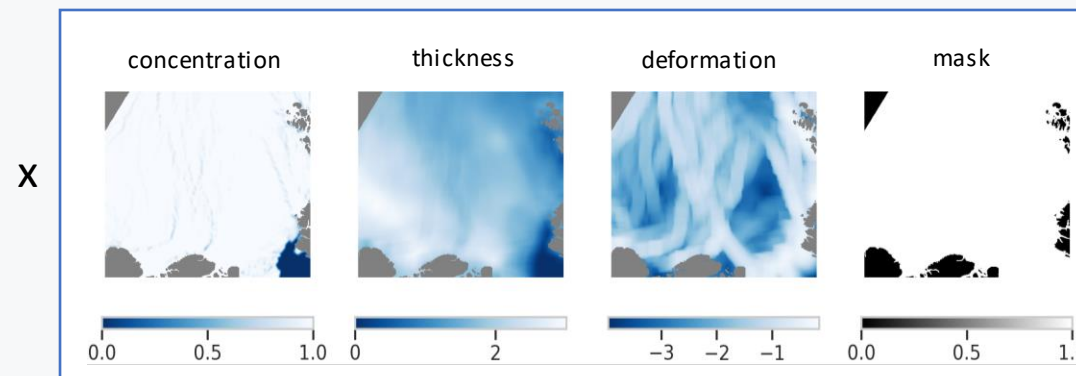
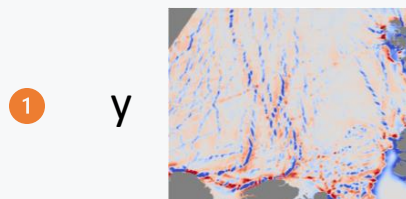
Implementation details



Model Residual Neural network $f(x,z,t)$

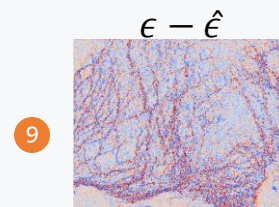
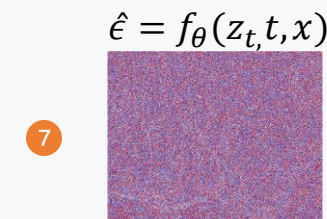
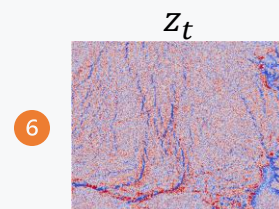
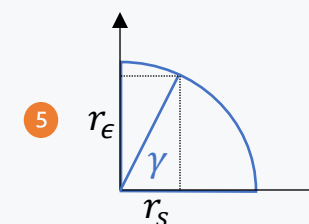


Training algorithm



For one sample

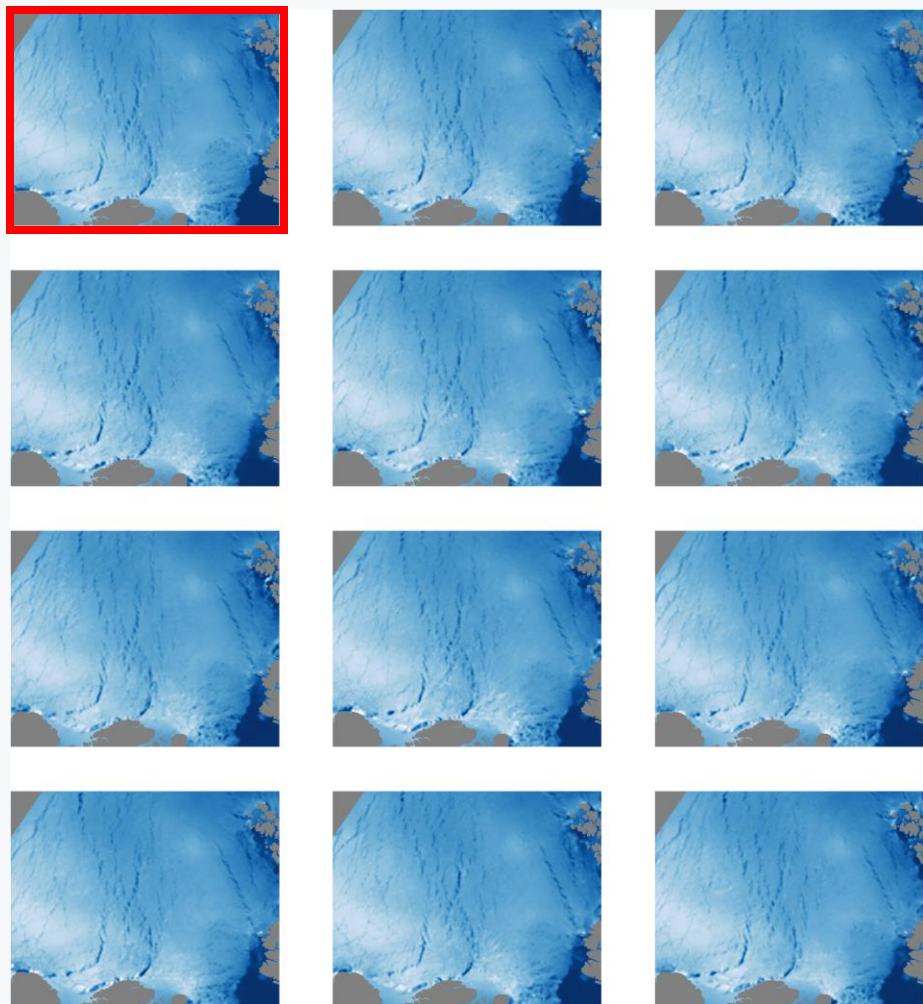
1. Draw a HR image y and a LR context x in the training set
2. Draw a diffusion time t between 0 (full signal) and 1 (full noise)
3. Draw a white Gaussian noise ϵ
4. Compute diffusion angle: $\gamma = \gamma_{min} + t \cdot (\gamma_{max} - \gamma_{min})$
5. Compute the signal and noise rate: $r_s = \cos \gamma$, $r_\epsilon = \sin \gamma$
6. Compute the noisy image: $z_t = r_s \cdot y + r_\epsilon \cdot \epsilon$
7. Predict the noise by the NN: $\hat{\epsilon} = f_\theta(z_t, t, x)$
8. Predict the image: $\hat{z}_{t-1} = (z_t - r_\epsilon \cdot \hat{\epsilon}) / r_s$
9. Compute the loss on the noise: $= L(\theta) = \|\epsilon - \hat{\epsilon}\|^2$
10. Minimize L



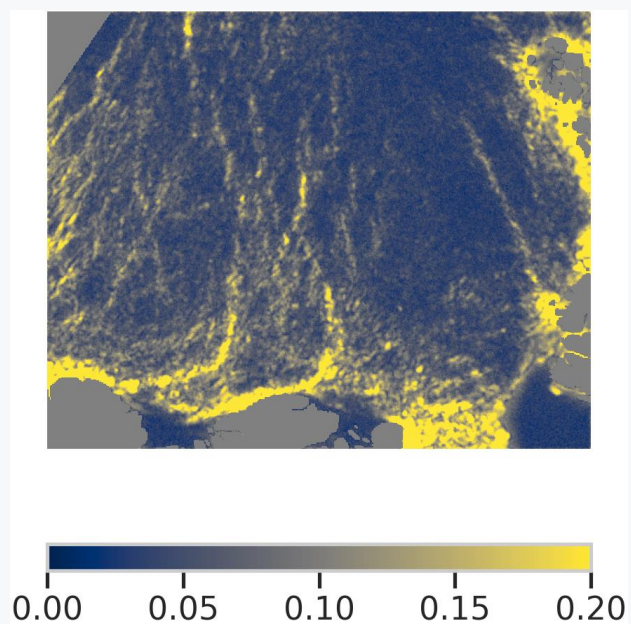
A stochastic generator

The generated process depends on the noise and enable to generate an ensemble of likely high-resolution images.

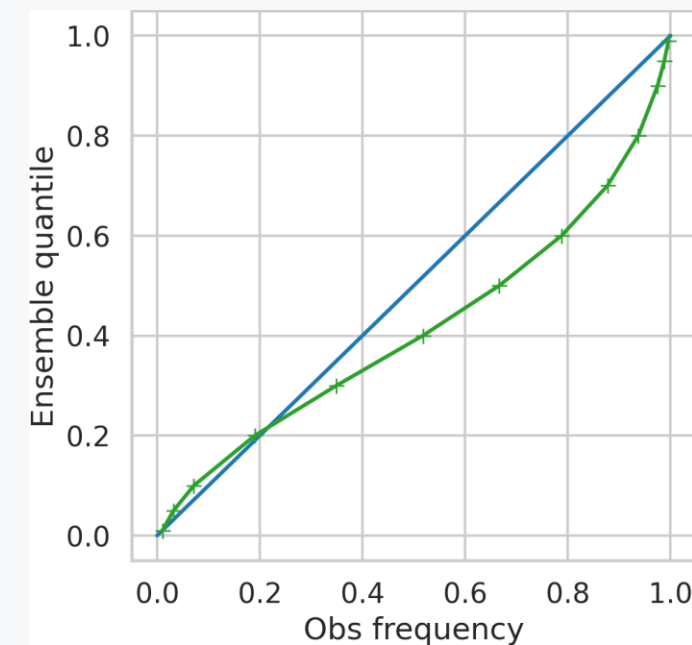
True image



Spread

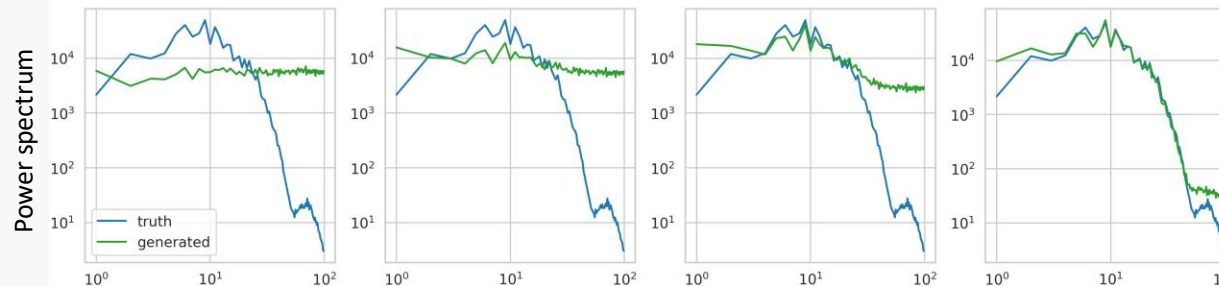


Reliability

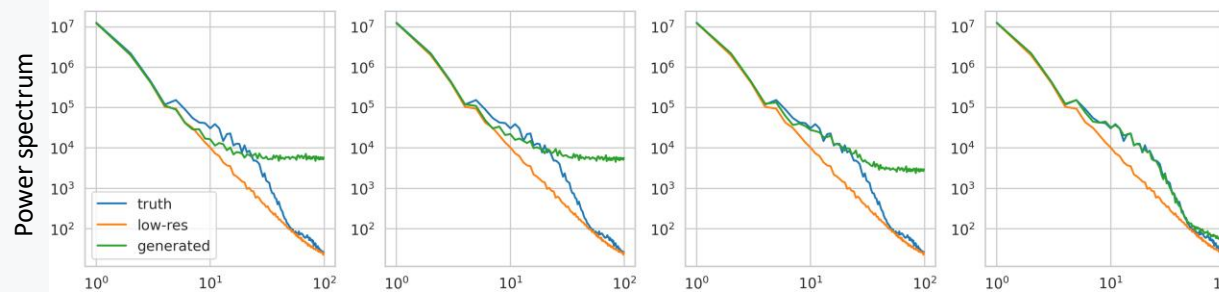
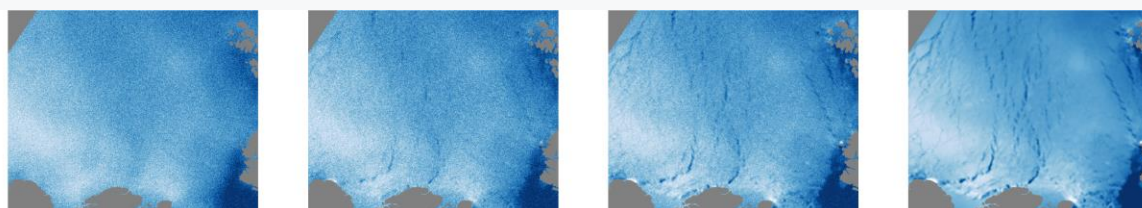


Preliminary result

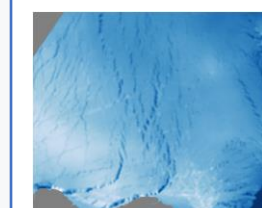
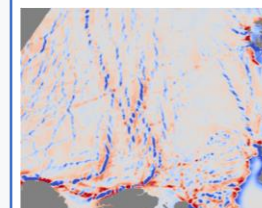
Generated field in anomaly
(SIT HighRes – SIT LowRes)



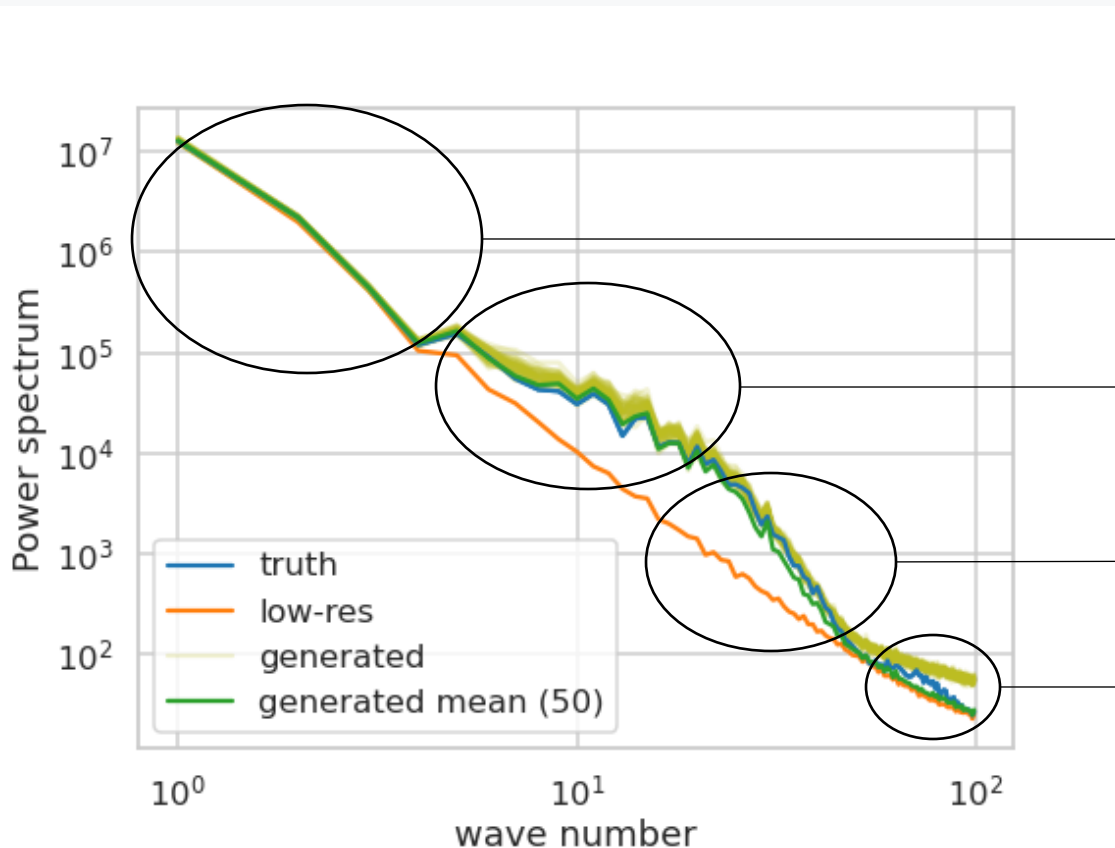
Generated SIT fields



TARGET



More on power spectrums



Large-scale

Low-res = high-res

medium-scale (fully deterministic and predictable)

Ensemble mean > Ensemble members

Fine-scale (probabilistic)

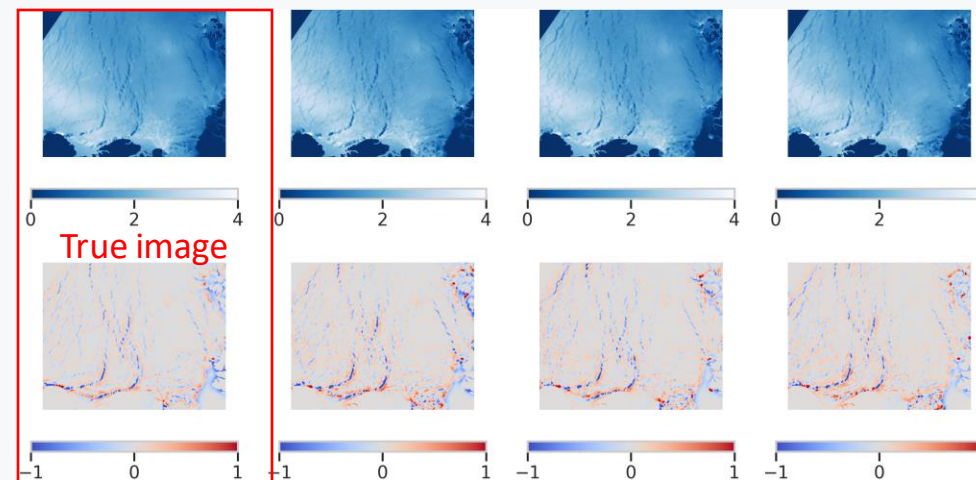
Ensemble members > Ensemble mean ?

Finest-scale (probabilistic and unpredictable)

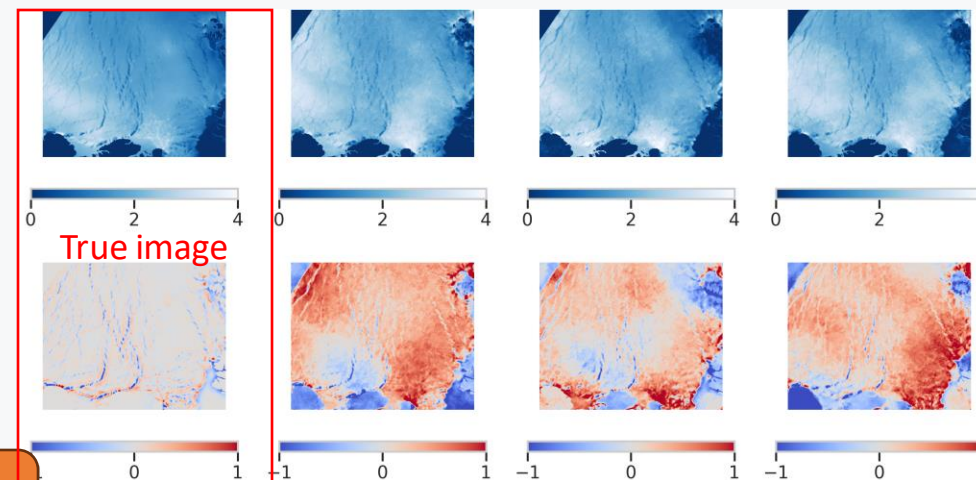
Ensemble mean = Low-res

Anomaly Vs full field generation

Anomaly generation



Full-field generation



Full-field induces large-scale biases

- **Diffusion models can be used to generate a realistic sea ice thickness field**
- Many implementation choices have been made:
 - Dataset creation: smoothing
 - Choice of input features: guided by observable variables
 - Model architecture: Residual UNET
 - Diffusion type: continuous time
 - Training: Loss computed on the noise
 - Generation: deterministic generation (the noise is only drawn once)
 - Many hyperparameters
- What is the more sensitive choice?
- Next step: inference with observation data